# A BRIEF TOUR OF ECONOMIC EPIDEMIOLOGY MODELLING

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## A Brief Tour of Economic Epidemiology Modelling

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#### Abstract

Prior to the Covid-19 crisis, the integration of epidemiology and economics that is, economic epidemiology modelling (epi-econ) in literature was relatively limited. The first fully integrated general equilibrium model, (Goenka et al., 2014) was published in the *Journal of Mathematical Economics (JME)*. The emergence of the Covid-19 crisis has prompted an unprecedented surge in the epi-econ literature. The *JME* has actively contributed to this area by publishing a special issue on epi-econ modelling (Volume 93) and publishing papers within this area. This survey primarily explores these *JME* papers along these lines: macroeconomics and policy, microeconomics and economic behavior, and mathematical advances. The survey looks ahead to some emerging areas in this literature.

Keywords: Economic epidemiology, Covid-19, pandemics, infectious diseases, NPI, optimal control, lockdowns.

JEL Classification: E13, E22, D15, D50, D63, I10, I15, I18, O41, C61.

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## 1 Introduction

The Covid-19 crisis which emerged in early 2020 triggered an unprecedented surge in the so-called economic epidemiology, *epi-econ* literature, namely integrated mathematical epidemiological and economic models. This is not entirely due to the number of fatalities (over 6 million) which is far below those caused by other major epidemics like AIDS-HIV.<sup>1</sup> What does explain the upsurge of this literature are the high number of infections in a matter of weeks by a novel virus which caused significant mortality and for which there was no known prevention or cure. The pandemic significantly affected labor supply, disrupted normal activity, and the fast diffusion of the virus led to a breakdown of critical supply chains across the globe. The economic toll was immediate. In the absence of prophylactic measures such as vaccines or proven treatment in the early phase of the epidemic, governments resorted to so-called Non-Pharmaceutical Interventions or NPIs, including full lockdowns, to stop the explosive dynamics of infections. There was a concern whether the NPIs would only compound the economic costs or whether controlling infections will reduce eventual economic losses: i.e. is there a health versus wealth trade-off? Indeed, whether a general lockdown is desirable from a social welfare, rather than public health perspective, is a key issue that has motivated this new literature. Economists and policymakers had to quickly learn more about the mechanics of epidemiological transmission. The epi-econ stream has exploded since the Covid pandemic, and is likely to continue developing over the next decades given that more pathogens are expected to emerge.

The desirability and efficacy of lockdowns has remained controversial. Contact tracing was effective in East and South East Asian economies because systems were already in place from prior pandemics and attempts to install them in countries such as UK were expensive failures. They also require access to private information which can be problematic for many economies. Dobson et al. (2023) argue that the primary health measures to control outbreaks in the period before vaccines become widely available to control a novel pathogen, are isolation of susceptible hosts and testing for infection once tests have been developed and distributed. These issues are likely to become salient with emergence of new pathogens.

Till the Covid-19 crisis, the epi-econ literature was comparatively thin. The classical appraisal of the economic impact of epidemics belongs to what we could label the economics of disasters. Probably one of earliest and most famous works in the field is that of Hirshleifer (1966) on the Black Death (1348-50).<sup>2</sup> Following Hirshleifer, the analogy between wars and epidemics has made in more recent publications: an epidemic (resp. a war) is associated with relative scarcity of human (resp. physical) capital. The typical research question concerns the nature of transitional dynamics involved by the latter imbalance effects following an initial epidemic shock (or war), thus restricting the analysis only to short-lived epidemics (see Mulligan and Sala-i Martin, 1993, for example). The above formalisation of epidemic shocks, typically in two-sector growth models, makes incorporating the supposedly related central concept, health, and its companion, health policy, challenging. It was with the emergence of

<sup>&</sup>lt;sup>1</sup>Some authors like Adam (2022) argue that the true figure is around 20 millions. Even if that turns out to be true, it would be significantly below the toll from other recent outbreaks.

<sup>&</sup>lt;sup>2</sup>Among several interesting conclusions, including the role of the Black Death in the demise of feudalism, Hirshleifer addressed a serious consideration: "Direct inferences can hardly be drawn from this 14th century catastrophe as to possible consequences of thermonuclear war..." (page 40).

one enduring epidemic, HIV/AIDS, that health expenditures (private or public) and health policy and systems became central to the economic modelling of epidemics. Scores of papers have been devoted to the evaluation of the short- versus long-term effects of AIDS, and the inherent (optimal) prevention/treatment public policies (see Azomahou et al., 2016, revisiting a much earlier work by Cuddington and Hancock, 1994).

Even though the economic modelling of epidemics markedly improved from the nineties, few papers incorporated infection dynamics in their analysis (see Section 3). Indeed, prior to the Covid-19 crisis, the vast majority of economic research on epidemics typically focused on the economic and social impact of epidemics through their morbidity and mortality effects. Morbidity effects decrease productivity and savings (via sustained health expenditures) as in the quasi-accounting frame proposed by Cuddington and Hancock (1994). Mortality is even trickier since in addition to its effect on labor supply, it may lead to lower schooling via the so-called Ben Porath effect (see Azomahou et al., 2016, Chakraborty et al. (2010)) and even impact the fertility rate (See Aksan and Chakraborty (2014), Boucekkine et al. (2009) and Young, 2005) via a general equilibrium effect increasing female participation in the labor market. Of course, these effects may hardly play evenly across social classes, thus leading epidemics to potentially deepen inequalities (see Chakraborty, 2004 and Boucekkine and Laffargue, 2010). The papers cited above pay minimal attention to the dynamics of infections, and even less to the inherent mathematical epidemiology literature. When infection dynamics are introduced, they are done in a different time-frame as in Chakraborty et al. (2010).

There was a literature that did take infection dynamics seriously and introduced compartmental epidemiology dynamics to economic models prior to the Covid pandemic (see Section 3).<sup>3</sup> This was concerned with endemicity of diseases such as HIV-AIDS, Malaria, Tuberculosis, and SARS-CoV-1. The joint modelling of economic and epidemiology should be possible in principle as both are described by dynamical systems but as we explain below, epi-econ models are technically difficult to analyse rigorously in intertemporal environments: the disease dynamics are naturally non-convex so that existence and sufficiency in optimal control settings is not guaranteed. The dimensionality is also higher than their standard dynamic economic counterparts due to the additional state variables for disease dynamics.

The first genuinely epi-econ model with capital accumulation and health expenditures in dynamic general equilibrium framework was published in the *JME* in Goenka et al. (2014). In this paper, there is a joint evolution of economic and disease dynamics which was absent in the earlier papers and is a characteristic of the new epi-econ literature that has emerged. The mathematical challenges and issues from integrating the non-convex disease dynamics are addressed. How optimal control of the disease depends on economic and disease characteristics is analyzed in the the paper. Thus it addressed many of the modelling issues that became salient in the recent literature, and We shall use it as a benchmark in this paper (see Section 3) after a brief introduction to mathematical epidemiology.<sup>4</sup>

The outbreak of Covid raised new modelling issues. While the Journal of Mathematical

<sup>&</sup>lt;sup>3</sup>See Bonds et al. (2010), Bosi and Desmarchelier (2018), Delfino and Simmons (2005), Gersovitz and Hammer (2004), Goenka and Liu (2012, 2020), Goenka et al. (2014).

<sup>&</sup>lt;sup>4</sup>The earlier paper (Goenka and Liu, 2012) which modelled the the effect of infectious diseases on the economy but not their full joint determination, discussed ad-hoc use of non-pharmaceutical interventions such as imperfect vaccines and isolation to control the disease.

*Economics* had not contributed much to the theoretical literature on the socioeconomic consequences of mortality,<sup>5</sup> it has become since become an important outlet for the epi-econ literature. Since the Covid-19 outbreak, the Journal has also devoted a full special issue (Volume 93) to epi-econ modelling applied to the Covid crisis with 19 contributions (see Boucekkine et al., 2021 for an overview), one of the very first Covid special issues published in economic journals. Since then, *JME* has continued publishing high quality contributions to the epi-econ stream.

The plan of the survey is as follows. After a brief introduction to epidemiology modelling (Section 2) and the pre-Covid epi-econ literature (Section 3), we review this *JME* literature in Section 4,5, and 6, along three distinct lines: macroeconomics and policy, microeconomics and behaviour issues, and technical problems arising in epi-econ modelling. Section 7 briefly highlights some emerging areas in epi-econ and concludes.

## 2 A primer on epidemiological models

Epidemiology models provide a structured approach to understanding the dynamics of infectious diseases within populations. In these models, individuals are classified into distinct compartments or health states based on their disease status. Typically, the commonly employed compartments include Susceptible (S), Infected (I), and Recovered (R). The movement of individuals between these compartments is governed by a set of mathematical equations representing the transmission, progression, and recovery of the disease. This compartmentalized approach allows us to analyze and simulate the spread of infectious agents, assess the impact of interventions, and inform public health strategies to control and manage infectious diseases. In this section, we briefly review the epidemiological models frequently incorporated in the *epi-econ* literature. Additionally, we explore specific issues that affect our understanding of the interplay between disease transmission and the economy.

The SIS Model The SIS model was used extensively in the pre-Covid literature as the focus was on diseases such as malaria and TB where recovery from one bout of infection could lead to subsequent re-infections. The total population, N, is divided into two groups: the susceptible S and the infected I. Individuals are born at the rate b, healthy and susceptible to the disease. Birth is understood to mean entry to the population either through birth or migration. The usual assumption is homogeneous mixing so that the likelihood of any individual contracting the disease is the same.<sup>6</sup> There is horizontal incidence of the disease i.e. transmission from peers. Let  $\alpha$  be the average number of adequate contacts of a person to catch the disease per unit time or the contact rate. Then, the number of new cases per unit of time is  $\alpha(I/N)S$  and depends on the fraction of the infected. The contact rate  $\alpha$  is the key

<sup>&</sup>lt;sup>5</sup>The Journal has published articles in a few theory areas such as life-cycle consumer with endogenous survival and other mathematical demography problems (e.g, Kuhn et al., 2011, or Cai and Lau, 2017), optimal population size problems and other population ethics issues involving mortality (see Boucekkine et al., 2014 or Fleurbaey et al., 2014), and the study of the relationship between pollution, mortality and optimal environmental policy (see Goenka et al., 2020 among others.)

<sup>&</sup>lt;sup>6</sup>Thus how individuals choose interaction (e.g. Kremer (1996)) is abstracted from. The choice of who to interact with is significant for STDs but much less so for other infectious diseases.

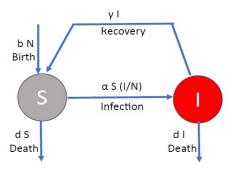
parameter and reflects two different aspects of disease transmission: the biological infectivity of the disease and the pattern of social interaction. Changes in either will change  $\alpha$ . The recovery of individuals is governed by the parameter  $\gamma$  and the total number of individuals who recover from the disease at each time period is  $\gamma I$ . Upon recovery, individuals move back to the class of susceptible individuals.<sup>7</sup> Each individual faces the exogenous death rate, d, irrespective of health status.

Figure 1 describes the transfer diagram for the *SIS* model. And the dynamics is given by the following system of differential equations:

$$S = bN + \gamma I - \alpha (I/N)S - dS$$
  
$$\dot{I} = \alpha (I/N)S - \gamma I - dI$$
  
$$N = S + I$$

This SIS model can have two steady states: disease-free steady state and disease-endemic steady state. <sup>8</sup>

Figure 1. The Transfer Diagram For the SIS Epidemiology Model



Note: In a SIS epidemiology model, the total population is divided into two groups: the susceptible denoted as S and the infected denoted as I. The birth rate is b and newborns are born healthy and susceptible. All individuals irrespective of health status die at the rate d. The susceptible get infected at the rate  $\alpha \frac{I}{N}$  and the infected recover at the rate  $\gamma$ .

**The SIR Model** In the SIRS model, the total population, N, is divided into three groups: the susceptible S, the infected I and the recovered R. Different from the SIS model, the SIRmodel makes the alternative assumption that on recovery from the infection and individual gains immunity from subsequent re-infections at the rate  $\gamma$  and will never get re-infected.

<sup>&</sup>lt;sup>7</sup>Upon recovery, individuals may or may not develop immunity to the disease. Even if they acquire immunity, they are still susceptible to mutations of the disease, or other types of infectious diseases. One of the leading examples is influenza, the virus for which mutates with new strains discovered each year. Immunity from one type of flu does not typically confer immunity to other strains. Reinfections proved to be a key to understanding the evolution and control of Covid.

<sup>&</sup>lt;sup>8</sup>Disease-free steady state exists for all parameter values, while disease-endemic steady state exists only when  $\frac{b+\gamma}{\alpha} < 1$ . When both steady state co-exist, that is  $\frac{b+\gamma}{\alpha} < 1$ , the disease-free steady state is unstable. In this Figure, disease related mortality is not modelled.

This is an accurate description for diseases such as chicken-pox, measles, etc. which are now controlled by widely used vaccines. The SIR model is given by the following system of differential equations:

$$\dot{S} = bN - \alpha(I/N)S - dS$$
  
$$\dot{I} = \alpha(I/N)S - \gamma I - dI$$
  
$$\dot{R} = \gamma I - dR$$
  
$$N = S + I + R$$

As in the SIS model, there can be two steady states - disease-free steady state and disease-endemic steady state.<sup>9</sup>

In the recent *epi-econ* literature there was a concern of lockdown policies in anticipation of introduction of vaccines which was hoped to end the Covid-19 pandemic. These models were very short run models and it was assumed that in a lockdown, there would be no movement in and out of the population. Thus, the birth rate, b, (interpreted broadly as entry of new individuals due to birth, migration, mobility) and death rate, d, (interpreted broadly as biological death from other causes, or exit from population) were set to zero.

The SIRS Model While the early Covid-19 pandemic models both in the epidemiology (see Ferguson et al. (2020)) and economics literature assumed SIR dynamics, with time it became clear that the immunity from prior infection as well as vaccinations was not long lasting. The SARS-Cov-2 virus is not a stable virus such as the ones that cause measles and small-pox, and mutations of the virus imply that while there is a period of immunity to a subsequent re-infection, there is also escape from immunity and re-infections. Thus, a SIRS framework may be a more satisfactory one to model Covid-19 pandemic. That is, we assume that recovered individual may lose immunity and become susceptible to the disease at the rate  $\psi$ . The transfer diagram for the SIR epidemiological models is shown in Figure 2. and the model is given by the following system of differential equations :

$$\dot{S} = bN - \alpha(I/N)S - dS + \psi R$$
  

$$\dot{I} = \alpha(I/N)S - \gamma I - dI$$
  

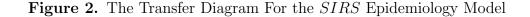
$$\dot{R} = \gamma I - dR - \psi R$$
  

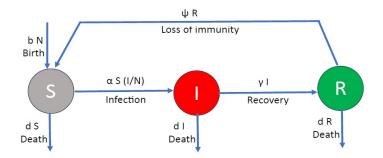
$$N = S + I + R$$

There are two steady states and as in the other cases the disease-free steady state always exists and there will be a disease-endemic steady state if  $\frac{b+\gamma}{\alpha} < 1.^{10}$  The *SIR* dynamics where there is no escape from immunity is a special case of the *SIRS* dynamics with  $\psi = 0$ . However, the implications for disease control are entirely different in the *SIR* and *SIRS* as

<sup>&</sup>lt;sup>9</sup>Disease free steady state always exists. It is stable when  $\frac{\alpha}{b+\gamma} \leq 1$ , and unstable when  $\frac{\alpha}{b+\gamma} > 1$ . When  $\frac{\alpha}{b+\gamma} > 1$ , there exists a unique endemic steady state, which is stable. The equations describing the steady states are quadratic, the steady state is unique and does not exhibit any complex dynamics. (See Busenberg and Van den Driessche (1990), Goenka et al. (2021), and Mena-Lorcat and Hethcote (1992)).

<sup>&</sup>lt;sup>10</sup>The stability properties are similar to the other two models.





Note: In a *SIRS* epidemiology model, the population is divided into three groups: the susceptible denoted as S, the infected denoted as I, and the recovered R. The birth rate is b and newborns are born healthy and susceptible. All individuals irrespective of health status die at the rate d. The susceptible get infected at the rate  $\alpha \frac{I}{N}$ , the infected recover at the rate  $\gamma$ . The recovered may lose immunity at the rate  $\psi$ . The *SIR* dynamics where there is no escape from immunity is a special case of the *SIRS* dynamics with  $\psi = 0$ .

in the former individuals gain permanent immunity but not in the latter. Thus, implications for individual behavior and aggregate dynamics are entirely different Goenka et al. (2024c).

**Challenges in choice of epidemiology models** The epidemiology models above are biological frameworks employed by epidemiologists, assuming the disease transmission dynamics as a given factor. Here, we address certain considerations in the selection of epidemiological models by economists. The decisions regarding the structure and intricacies of epidemiological cal models integrated into eco-epidemiological frameworks hinge on the nature of the disease and the specific research question at hand. Such choices inevitably influence model design, equilibrium outcomes, and hence, policy recommendations.

Choice of compartments: The SIR model has been widely used in the context of Covid. However, when emphasizing interventions like contact tracing or testing, the group of exposed individuals, denoted as E, becomes important, as they are asymptomatic and infectious. Likewise, the group of vaccinated individuals, denoted as V, is crucial if vaccinations are modelled, but is less relevant otherwise. Various *epi-econ* models differ in which health states are used and the details of the dynamics between these states. In the latter part of the pandemic, as it became clear that disease related or vaccine conferred immunity is not long-lasting, SIRS models came to be used. Thus, the choice of which compartments to use is governed by the research question.

Transmission mechanism: There are two primary ways to model the transmission of infections. The one described above is the standard incidence model where new infections depend on the fraction of infected. The other is the mass action model (simple Kermack-McKendrick model) where infections depend on the number of infected so new infections are given by  $\alpha SI$ .

If N is fixed then the two models are essentially similar.<sup>11</sup> When population is not constant either due to longer horizons where birth and deaths become significant, or the population is not closed so that there are movements in and out due to mobility, migration, etc. or there is disease related mortality the choice of which model to use becomes significant. The epidemiology literature tends to use the standard incidence model (or some variation of it) for several reasons. There are also reasons why one would like to consider its use in economic models. First, the mass action model has a scale effect so that increases in population size will increase the rate of infections as the contacts increase linearly with population size  $(\alpha N)$ . However, the pattern of human interaction is relatively stable and invariant to population size. Second, Anderson and May (1991) estimated the contact rate for 5 diseases for population size 1,000 and 400,000 using the specification  $\alpha N^{\nu}SI/N$  and found that  $\nu \approx (0.03, 0.07)$  indicating that the standard incidence model is a better fit than the mass action incidence model. Third, as mortality increases in the mass action model there is an in-built dampening mechanism - as population size drops, so does the contact rate. Thus, the first model will imply a self-limiting behavior of epidemics due to mortality when the second will not. Fourth, if population is not growing then the threshold for existence of an endemic steady state depends inversely on initial population size - so that a larger initial condition makes it more likely the disease will be endemic (Mena-Lorcat and Hethcote (1992)). Furthermore, if population is growing then eventually every one will get infected except when disease related mortality is higher than the natural population growth rate (Mena-Lorcat and Hethcote (1992)).<sup>12</sup>

Population dynamics: In the recent literature in the early part of the pandemic there was a concern of lockdown policies in anticipation of introduction of vaccines which was hoped would end the Covid-19 pandemic. These models were very short run models and it was assumed that in a lockdown, there would be no movement in and out of the population. Thus, the birth rate, b, (interpreted broadly as entry of new individuals due to birth, migration, mobility) and death rate, d, (interpreted broadly as biological death from other causes, or exit from population) were set to zero. Over time it has become clear that both vaccine and disease conferred immunity is not long lasting. Even though disease related mortality has declined, the disease has persisted so attention will shift to medium and longer run consequences. In this situation, treating the population as fixed will need to be re-considered. There will be the related issue of whether to use the mass action or standard incidence model as their longer run implications differ for changing populations.

Timing of disease related mortality: Most of the models that incorporate mortality of those infected, did so in what can be called a model of early mortality - the infected die at the rate  $\phi$  due to infectious diseases. An alternative specification, a model of delayed mortality, the recovered die at the rate  $\phi$  due to infectious diseases. This conforms to a situation

<sup>&</sup>lt;sup>11</sup>In the first model, the number of contacts is  $\alpha N$ , and the probability of a contact of an infective with a susceptible is  $\alpha N(S/N)$  giving the number of new infections  $\alpha N(S/N)I = \alpha SI$ . In the second model, the number of contacts for a susceptible to catch the disease as  $\alpha N(I/N)$  giving the number of new infections as  $\alpha N(I/N)S = \alpha SI$ .

<sup>&</sup>lt;sup>12</sup>See Mena-Lorcat and Hethcote (1992), Hethcote (2000), and Keeling and Rohani (2008) for further discussion of the modeling in SIR models.

where those infected have been isolated or hospitalised so their mortality does not affect new infections in the populations. In the first model, if mortality is high the period of infectiousness is reduced which in turn will reduce new infections.<sup>13</sup> Thus, there is a self-limiting effect of increase in mortality. Goenka et al. (2021) compare these two specifications and find that the optimal policies greatly differ depending on which specification is used as in the first specification the self-limiting effect on infections of mortality leads to policy inaction.

Discrete or continuous time: Epidemiology models are frequently developed in both continuous and discrete time. Is it significant in choosing one over the other? In macroeconomic analysis usually discrete time formulations are used as the time-series macroeconomic data is available at quarterly frequency. For fast-moving epidemics or emerging diseases, this may be too slow a frequency. Thus, most of the epidemiology literature tends to use continuous time formulations. There is another reason for thinking about the time-frequency of the models. The dynamics in the simple SIS, SIR and SIRS model do not exhibit any complex dynamics (Busenberg and Van den Driessche (1990) and Mena-Lorcat and Hethcote (1992)). The situation in discrete time is very different. Allen (1994) shows that there can be cycles in the same models in discrete time. Goenka and Liu (2012) show that in the SIS model the dynamics are topologically conjugate to the logistic map with the bifurcation parameter is the contact rate,  $\alpha$  and increasing it induces flip-bifurcations and topological chaos. From the Poincaré-Bendixson theorem, this cannot happen in the SIS model in continuous time as it is a 1-dimensional system or in simple SIR or SIRS models as these are two-dimensional systems in closed, bounded regions (the interval [0,1]). Thus, which frequency to choose can give different implications if infectiousness of the disease is high enough.

## **3** Pre-Covid epi-econ models

The recognition of diseases such as malaria and tuberculosis, along with the increasing complexities posed by HIV/AIDS, sparked the development of early models integrating insights from the well-established epidemiological literature into the economics. This evolution led to the creation of fully integrated general equilibrium models that seamlessly blended epidemiological and economic frameworks. Concurrently, a related strand of work emerged in the epi-econ literature, displaying a contemporary focus shifting away from the dynamics of infections and epidemics to delve into behavioral effects and intergenerational issues. This section offers an overview of all these *epi-econ* models predating the COVID era.

**Early works** These first epi-econ models in a compartmental epidemiology framework generally looked at a one-way interaction where either the disease dynamics affected economic choices and outcomes or the other way around, but not a full two way interaction.

One of the first papers to model the interaction of epidemiology and economic choices was Geoffard and Philipson (1996). They study the decision problem of an individual to

<sup>&</sup>lt;sup>13</sup>To see this, note that new infections are due to fraction of I. The outflow from I is given by  $\gamma + d + \phi$ , which reduces the stock of infectives and thus, new infections.

take protective and preventive action in the face of an epidemic. A key insight is that protective behaviour is prevalence dependent and there is a threshold of disease incidence below which the inaction is optimal. The threshold is increasing in the discount rate and cost of protection, and decreasing in cost of infection and infectivity of the disease. As individuals make decisions taking into account their transitions from healthy (susceptible) to infected, the optimal decisions depend on the incidence of the disease in the population. Thus, while the hazard rate from susceptibles is increasing in fraction of infected in epidemiology models, it may be decreasing in models where individuals are making optimal protective decisions.

Whether individuals take into account the effect of their decisions on the aggregate disease dynamics is examined in the paper by Gersovitz and Hammer (2004). They look at prevention and treatment with different disease dynamics. As individuals are small relative to the population, they engage in "disease taking behavior", where they take disease incidence as given and ignore the effect of own actions on the population incidence. There can be prevention externalities<sup>14</sup> Unlike the earlier Kremer (1996) paper, the decision maker takes into account how current actions affect evolution of the health status of the household. Like Geoffard and Philipson (1996), the paper is a partial equilibrium model where the the economic variables are taken as given and not affected by the incidence of the disease.

The contemporaneous paper of Goldman and Lightwood (2002) also studies the optimal decision for treatment in a partial equilibrium SIS framework. This paper also identifies the treatment externality and shows that the effect on incidence can be substantial. It shows that the cost minimizing programme has lower treatments when disease incidence is high.

In these papers the disease incidence affects the welfare of individuals and its control is the focus but the effect of the disease on economic outcomes is not modelled. The effect of incidence of the disease on economic outcomes was studied in the first macroeconomic models where disease affects the participation or productivity of the workers ((Bonds et al. (2010), Delfino and Simmons (2005) and Goenka and Liu (2012)). Bonds et al. (2010)) used a Solow growth model where disease incidence reduces labor supply and show a multiplicity of the steady state which arises from the two steady states in the pure epidemiology SISmodel. The steady state where the disease is incident is interpreted as the poverty trap. Delfino and Simmons (2005) also use a Solow model with SIS disease dynamics. In addition they add a term to the dynamics of the susceptibles where the growth rate depends on the susceptible versus the infective population as in a Lotka-Volterra model rather than a constant birth rate. This generates dynamics driven by the predator-prey assumption on growth of susceptibles.

While these papers explore the macroeconomic effects of pandemics they are not able to address three important issues: how disease incidence affects savings decisions, labor supply, and welfare implications. Goenka and Liu (2012) use a neoclassical growth framework with endogenous labor-leisure choice in discrete time rather than a Solow-type model with constant savings rate. This allows a discussion of welfare effects that cannot be made in the other two models. The paper shows that there are both extensive margins on labor supply: the infected population's labor productivity drops, as well as intensive margin effects. If the usual assumption on positive cross-partials in the utility function is made then labor supply

<sup>&</sup>lt;sup>14</sup>The externalities associated with vaccinations were also identified by Brito et al. (1991) and Kremer (1996) and treatment externalities of the effect of health behavior on the population incidence are ignored.

of the susceptible behaves in a similar way to the standard real business cycle model. When aggregate infections are high, it decreases as there is lower productivity. It turns out that in discrete time, the standard *SIS* dynamics are topologically conjugate to the logistic map and the infectivity rate is the bifurcation parameter. When there is topological chaos, the model appears as if it is a standard real business cycle model with white noise exogenous shocks. There is a fundamental difference between the economic epidemiological model and the real business cycle as in the former there is a dynamics of the labor productivity i.e. the disease dynamics which can be controlled. In the latter case, these shocks are truly exogenous. They explore how to stabilise the fluctuations using ad-hoc interventions<sup>15</sup> such as imperfect vaccinations and isolation of infected. These perturb the rate of infection to target the desired steady state level of infections. This paper is the first paper in the economics literature to explicitly model using NPIs to control epidemics. The gains from stabilizing the fluctuations in the economy are non-trivial.

**First-generation integrated** *epi-econ* **models** The first paper to fully integrate the compartmental epidemiology model in a dynamic general equilibrium framework with a two way interaction is Goenka et al. (2014), published in this journal. This paper uses a neoclassical growth model where households can invest in physical and health capital when there is an infectious disease that impairs workers productivity circulating in the population. The health expenditures could be anything that either control the spread (preventive expenditures) and speed up recovery (curative expenditures). To allow for generality of thinking about control of the disease so as to cover diverse aspects such as investment in sanitation, hospital beds and ventilators, etc. the paper allows for partial depreciation of health capital. If there is full depreciation, then the interpretation is consistent with social distancing as this is a consumption and utility reducing expenditure solely aimed at controlling infections (see Eichenbaum et al. (2021) who also make this interpretation). There can be three steady states in the economy: where the disease is eradicated, and where it is endemic with positive or zero health expenditures. The choice of the health expenditures depends on the relative magnitude of marginal productivity of physical capital investment and health expenditure. The marginal productivity of health expenditure can be interpreted as the marginal contribution of health capital on effective labor supply. Essentially we can think there is an intermediate production function which transforms one unit of health expenditure into labor supply through the effect on endogenous disease dynamics. The paper shows that when infectious disease incidence is low, it is optimal not to accumulate any health infrastructure to control them. This was manifest in the Covid-19 pandemic where high income countries that had no recent experience of pandemics were largely unprepared for it despite high per capita health expenditure which are geared more towards non-infectious diseases. The paper also shows that policy inaction can be optimal if disease incidence is too high or if capital stock is too low. Thus, economies which are likely to be most afflicted by infectious diseases may also optimally choose not to control it as the returns to labor are low and to investment are higher elsewhere.

This paper is the first to address and resolve the issues that arise from integrating nat-

<sup>&</sup>lt;sup>15</sup>Ad hoc in the sense that the interventions are not the solution to a maximization problem but using perturbation of the contact achieve a specified steady state level of infection.

urally non-convex disease dynamics into an optimal control framework. The Arrow and Mangasarian sufficiency conditions do not apply as noted earlier by Gersovitz and Hammer (2004) and Goldman and Lightwood (2002). None of the optimality conditions in the literature apply, and in fact, it is not even clear if the model has a solution. This is discussed in further detail in Section 6.

They characterise stability of the steady states and give sufficient conditions for local stability. In addition of the state variable for the disease, there are also for the physical and health capital which depend on optimal savings and health control decisions. It makes the system high dimensional (six) and while the local dynamics of disease free steady state echoes that of the pure epidemiology model (as the optimal health expenditures are zero), the conditions for the disease endemic steady states with positive health expenditures are non-trivial. Bosi and Desmarchelier (2018) have a model where pollution causes an externality which increases the incidence of the infectious disease. There is no control of either pollution or the disease. The externality can lead to cycles in their 2 dimensional model.

This framework is extended to endogenous growth with human capital accumulation by Goenka and Liu (2020). They show robust empirical evidence that there are three clusters of growth paths: countries with higher growth and income, low incidence of infectious diseases, and high human capital accumulation proxied by schooling; middle income countries with lower growth, higher incidence of infectious diseases and lower schooling; and a group of countries in a poverty trap with little or no growth, low income, high incidence, and low schooling. They develop a model where households can accumulate physical, health, and human capital as in the Lucas growth model. They also model the disease externality as in Gersovitz and Hammer (2004) where individuals do not take into account their actions on aggregate dynamics an issue which became important in the Covid-19 pandemic where mandates were introduced for NPIs such as wearing masks, contact-tracing, vaccinations, etc. precisely because of these externalities. The model generates three balanced growth paths consistent with the facts. As in Goenka et al. (2014) paper, there is a marginal condition which simultaneously determines the amount of health capital and whether human capital is accumulated or not. In equilibrium, the amount of health expenditure is determined when the marginal return to it is zero but it could be one where there is either human capital accumulation or not which is dependent on the amount of disease incidence in the economy. The issue of human capital effects has not been studied sufficiently in the new theoretical literature even though there was a lot of policy interest on school closures. The paper shows that the disease externality has substantial effects on economic outcomes. The efficient amount of health expenditures can be decentralised but paradoxically for economies with the highest incidence in a poverty trap, the optimal policy may be again be inaction. Goenka and Liu (2020) show how the incidence of a disease decrease investment rates in physical, human and health capital. Their results show that there is no trade-off between health and wealth: lower health outcomes implies lower wealth outcomes.

**Related literature** A related body of work in the epi-econ literature that emerged contemporaneously is less interested in the evolution of infections and epidemics – indeed some do not even consider it – and more in behavioral effects and intergenerational issues.

An early contribution is Lagerlöf (2003) where exogenous epidemic (mortality) shocks

allow an economy to escape Malthusian stagnation. Closer to our lived experience, Young (2005)'s analysis of the HIV/AIDS crisis in sub-Saharan Africa identifies competing effects: while the reduction of the working-age population negatively affects economic growth, greater awareness and price effects increase labor force participation and health investment that positively affect growth. Boucekkine and Laffargue (2010), in contrast, explore the distributional and intergenerational implications of the HIV crisis. There, the adverse effects arise from lower parental investment in children and, especially dire outcomes for orphaned children. Not surprisingly, the effects are heterogeneous across the population and skill distribution. While none of these models incorporate feedback effect from human behavior to mortality, they anticipate the long-term and distributional effects, especially for child outcomes, that have become salient after Covid 19.

Low-frequency disease dynamics and two-way effects are considered in Chakraborty et al. (2010) who show, echoing Geoffard and Philipson (1996), that poorer societies tend to underinvest in prevention and the long-term economic cost of endemic diseases such as malaria and HIV is substantial. In contrast, the oscillatory pattern of outbreak and containment in Chakraborty et al. (2016) emerges from the two-way interaction between prevention incentives and disease prevalence and accounts for the regular emergence of epidemics through human history. Both papers numerically take into account the non-convexity problem that arises in epi-econ models. Finally, a different kind of distribution effect on chidren arises in Aksan and Chakraborty (2014). The authors exploit the multiplicity of stationary equilibrium of epidemiological models to study how prevention versus eradication efforts explain the high morbidity burden of sub-Saharan Africa's children and account for lower human capital investment and slower fertility transition.

This literature has continued to develop in parallel with the standard epi-econ literature. It remains to be seen how the experience of the recent pandemic and upsurge in alternative modeling strategies shape interest in intergenerational issues.

## 4 Covid-19 epi-econ literature: Macroeconomics and policy

In this section, we will emphasize some of the contributions of the *JME* to the recent Covid epi-econ literature. Of course, the intersection of this section with the quite substantial special issue (20 papers, including the extensive introduction to this issue) published by the Journal in March 2021 is more than significant. Several other epi-econ research papers have been published after the special issue, they are included in the discussion together with other relevant theoretical contributions outside the Journal.

In Section 2, a few basic epidemiological models were presented, Section 3 introduced to the pioneering work of Goenka et al. (2014) on integrated epi-econ models in dynamic general equilibrium setting. As the pre-Covid models discussed in Section 3 were concerned with endemic diseases and stationary states, the new literature arisen in response to the outbreak of a novel disease has focussed more on short-run dynamics. Some authors took a step further and introduced some special features of the Covid dynamics in the epidemiological component of their epi-econ model, others exploring other research questions kept on using the canonical SIR and similar models. For example, the role of asymptomatic individuals has been hardly accounted for in this literature (one exceptions is Aspri et al. (2021)),<sup>16</sup> nor the critical ICU (Intensive Care Units) constraint, which is in practice the rationale behind the wide use of lockdown policies. We will not review here the the vast number of epidemiological models that have been worked out in the Covid literature: compared to the models used in science journals (see for example, Dobson et al., 2023). They are for sure much smaller and parsimonious consistently with typical approach in economic theory to allow for at least a partial analytical approach. There is another important reason for the parsimonious nature of the epi-econ models as opposed to the epidemiology models. The latter largely do *simulations* and comparisons of scenarios which the economics literature wants to find the *optimal* policy. Thus, it is a control problem and the curse of dimensionality requires great simplifications. We summarize below some selected research lines.

Modelling NPIs, epidemic-economic linkages and optimal NPIs The incorporation of NPIs, in particular lockdown and testing,<sup>17</sup> into the epidemiological models, and later the epidemic-economic linkages, is not a big deal. In the early Covid epi-econ literature, the optimal epidemic control policies problems consisted basically in a replication of the Goenka and Liu (2012) and Goenka et al. (2014) framework where the infection rates and/or the recovery rates are made dependent upon the NPIs. For example, lockdowns are simply assumed to limit infection rates (just like health capital in the benchmark of this paper). Only a small fraction of the proposed models account for uncertainty despite its importance in the early months of the crisis.

In contrast, one of the more interesting refinements with respect to our benchmark is the introduction of age structures (in line with Kermack and McKendrick (1927) seminal model)<sup>18</sup> which allows the study optimal uniform versus targeted NPIs (for certain age classes only). This is highly relevant for an epidemic like Covid as mortality is concentrated in old ages. See Acemoglu et al. (2021) for an analysis of NPIs in an age-structured epi-econ model.<sup>19</sup> Only a handful of papers consider the whole set of NPIs in their analyses of optimal epidemic control policies.<sup>20</sup>

Lockdowns and the other NPIs would make sense in the absence of efficient vaccines. In the case of Covid, this is not a trivial question for an obvious reason: recovered (from infections) and vaccinated individuals are not immunized forever. Immunity from infection wanes as the virus mutates and infection from a prior strain does not confer immunity to another one, though severity of infection is reduced. An interesting model accounting for this crucial waning immunity property and for other relevant aspects of the Covid crisis is due to Caulkins et al. (2021) where epidemics dynamics interact with NPIs following the

<sup>&</sup>lt;sup>16</sup>This shouldn't be however considered as major defect from the theoretical viewpoint: a vast majority of this research builds on purely deterministic models while asymptomatics almost measure "the extent of our ignorance" to use a famous Solowian expression.

<sup>&</sup>lt;sup>17</sup>But also mask wearing, hand washing, and remaining at least one meter or so apart during an interaction. <sup>18</sup>See (Hethcote, 2009) for age-structured models in epidemiology

<sup>&</sup>lt;sup>19</sup>Gollier (2020) is another related interesting analysis although only scenario-based.

 $<sup>^{20}</sup>$ Alvarez et al. (2021) study optimal testing and lockdown policies, among a few other contributions. An interesting contribution to this line of work is Phelan and Toda (2022) who study how imperfect enforcement of NPIs is affected by the presence of imperfect pharmaceutical interventions such as testing.

equations below:

$$\begin{split} \dot{S}(t) &= \nu N(t) - \beta(\gamma(t), z(t)) \frac{S(t)I(t)}{N(t)} - \mu S(t) + \varphi R(t) \\ \dot{I}(t) &= \beta(\gamma(t), z(t)) \frac{S(t)I(t)}{N(t)} - (\alpha + \mu + \mu_I)I(t) \\ \dot{R}(t) &= \alpha I(t) - \mu R(t) - \varphi R(t) \\ \dot{\gamma}(t) &= u(t), \quad \gamma(0) = 1 \\ \dot{z}(t) &= \kappa_1 (1 - \gamma(t)) - \kappa_2 z(t), \quad z(0) = 0 \\ \gamma(t) \leq 1, \quad 0 \leq t \leq T \end{split}$$

where N(t) = S(t) + I(t) + R(t) is the total population. An interesting variation of the model with respect to the SIR is the term  $\varphi R(t)$ ,  $\varphi > 0$  which shows up in the dynamics of susceptible individuals: this means that any moment, recovered individuals are reinfected at rate  $\varphi$ <sup>21</sup> This corresponds to the SIRS epidemiological model described in Section 2. Two other ingredients of the model make it particularly relevant for the Covid outbreak. First of all, NPIs do not come without adjustement costs: in the overwhelming majority of epi-econ papers, the lockdown parameters can be adjusted without cost in continuous time (that's are continuous controls). In this frame, the intensity of the lockdown is given by  $1 - \gamma(t)$ ,  $\gamma(t)$  being the actual number of people working as a proportion of those who would normally be working. According to the fourth equation,  $\dot{\gamma}(t) = u(t)$  where u(t) is the employment rate,  $\gamma(t)$  is a state variable, not a jump variable. Very few papers introduce frictions in the NPIs, an example is Aspri et al. (2021).<sup>22</sup> Second, Caulkins et al. (2021) is one of the earlier papers putting forward the mental health aspect inherent in lockdown policies. In their setting, the infection rate  $\beta(\gamma(t), z(t))$  increases with  $\gamma(t)$  but it also increases with another variable, z(t), according to the last dynamic equation of the system above. Indeed, z(t) corresponds to fatigue due lockdowns. A more intense lockdown brings more fatigue, which make individuals less prone to comply with lockdown. This is of course largely implicit in the model above, we shall push this idea along a more micro-founded frame due to Adda et al. (2024) in Section 7.

Devising optimal NPIs requires the specification of an objective function. Typically, this implies balancing the economic cost of NPIs (loss of output generally) and human lives gained from NPIs. The more averse to human losses is the central planner, the more convex will be the objective function with respect to the number of the deaths (see for example Goenka et al. (2021)). In more applied work, it may be more convenient to specify the human cost due to death using established measures of the statistical value of life (see for example Alvarez et al. (2021) or Aspri et al. (2021)). Morbidity effects (for example reducing productivity as in the HIV-AIDS literature) are much less common. Productivity losses are however invoked in relation with Work-From-Home (WFH), a spreading practice in Covid

<sup>&</sup>lt;sup>21</sup>Another more extreme avenue to model loss of immunity at a lower analytical cost is to use a SIS model as in Bosi et al. (2021). This simplification is useful to come out with analytical results, which is the case of this paper framed in general equilibrium where individuals may care about the share of infected people.

<sup>&</sup>lt;sup>22</sup>In this framework, optimal lockdown policies are taken in the set of piecewise constant functions. Dobson et al. (2023) search for jointly optimal piecewise constant lockdown and testing policies.

times. This varies across occupations and individuals.<sup>23</sup> (Goenka et al., 2024a) also explore how the optimal lockdowns should be determined in a SIRS framework taking into issue ability to WFH, compliance with lockdowns, and the weight attached to disease related mortality. This extends the (Caulkins et al., 2021) who include mortality in the objective function but not in the state variables to fully account for disease related mortality including how change in population size affects discounting (see Section 6).

Within the class of optimal epi-econ frames surveyed above, once conveniently calibrated, a recurrent policy outcome in the absence of vaccines is that NPIs (and in particular lockdowns) are preferable to *laissez-faire* in the early stages of the outbreak. For example, La Torre et al. (2021) shows that in earlier stages, disease eradication by the means of NPIs is optimal but in the later stages it is not. This corresponds to the experience of COVID-19: some countries where the disease did not spread widely have largely been successful in suppressing it by actions in the early stages while other countries allowed it to and are struggling to do. This policy dilemma has been under discussion for a while given the apparent success of the Swedish herd immunity strategy till Fall 2020.<sup>24</sup>

From a more theoretical viewpoint, in particular regarding robustness of these optimal policies with respect to the deep parameters of the epi-econ models, things are much trickier: for example, Aspri et al. (2021) identify a sudden change in optimal policy as the statistical value of life is raised, from *laissez-faire* to a sizeable lockdown level. Again this is no surprise: as the value of life (or equivalently the degree of aversion to human deaths) rises, lockdowns are more likely to be the dominant strategy, by construction of the objective functions of the optimization problems. This is in line with the findings and analyses of many researchers in the field, in particular with Caulkins and his co-authors, who end up concluding: "Relatively small changes in judgments about how to balance health and economic harms can alter dramatically which strategy prevails. Indeed, there are constellations of parameters for which two or even three of these distinct strategies can all perform equally well for the same set of initial conditions...these complex dynamics emerge naturally from modeling the COVID-19 epidemic and suggest a degree of humility in policy debates". It is not difficult to identify one of the main sources of this complexity: a quick look at the state equations of the problem considered by Caulkins et al. (2021) listed above is enough to figure out the various non-concavity features they entail. We come back to this technical point in Section 6.

**Health systems** As alluded to above, the early optimal NPIs literature has not always accounted for the ICU capacity constraints (at the basis of the wide resort to lockdown policies) and has neglected quite often the hospitalization costs. This is clearly in contrast with the counterpart literature in public health.<sup>25</sup> We briefly present here two *JME* contributions

 $<sup>^{23}</sup>$ See Chopra et al. (2022) and Dingel and Neiman (2020) for example.

 $<sup>^{24}</sup>$ Another disputed policy debate is on the use of testing vs lockdowns as preferred NPIs. Dobson et al. (2023) outline the importance of the testing strategy (random or targeted for example) given the inherent testing capacity, highlighting possible cases where the joint use of lockdown and testing during a period of time may be optimal.

 $<sup>^{25}</sup>$ See Gallic et al. (2022) for a theoretically grounded empirical analysis of the sanitary policies that have been implemented in Europe in response to the two first waves of the COVID outbreak.

focused on the health systems with explicit ICU capacity constraints.<sup>26</sup>

A very nice analysis to start with is Loertscher and Muir (2021) that we present extensively for its originality and scope. The authors initially consider an elementary SIR model, and they impose an explicit state constraint according to which a fixed proportion, say  $\tau$ , of the infected people need to be hospitalized (or to get treated in an ICU). There is a fixed capacity constraint limiting access to the health system. The health policy considered is lockdown with the typical economic cost (depending on the intensity of the lockdown). The most original part of this contribution is the development of an epi-econ model with heterogenous agents. Each individual has a type,  $\theta$ , where  $\theta$  has a finite support. The lockdown policy is targeted in the sense that the intensity of the lockdown depends on the type  $\theta$ .<sup>27</sup> While the health system capacity constraint is on aggregate number of treated individuals of all types, the rate of treated may be type-dependent ( $\tau(\theta)$ ) just like the lockdown intensity. Furthermore, the parameter  $\tau(\theta)$  can be interpreted as the vulnerability of individuals of type  $\theta$  to the epidemic. Finally, labor productivity is type-dependent, which again a very relevant specification.

Loertscher and Muir (2021) derive several interesting results. Among other important results, their optimal dynamic lockdown policy imposes a specific short and sharp lockdown: the pandemic is allowed to spread till the ICU constraint binds, then a strict lockdown should be implemented for a period of time where the constraint remains binding, but with the policymaker easing the lockdown along the way. As outlined by the authors, ... "The qualitative features of the optimal dynamic lockdown policy differs substantively from those derived (Alvarez et al. (2021)). Their optimal dynamic policies have a "hump-shaped" appearance...with the policymaker gradually easing into and out of the lockdown. Accounting for heterogenous population, optimal policy requires a complete lockdown (that's with maximal intensity) for the more vulnerable and none on the less vulnerable. Acemoglu et al. (2021) also suggest targeted policies for different risk groups to limit infections, but Loertscher and Muir (2021) show how ICU capacity will determine the targeting strategy.

Miclo et al. (2022) is another strong epi-econ contribution explicitly accounting for the ICU capacity constraint. Precisely, the authors deal with an homogenous population facing an outbreak with SIR diffusion dynamics and they derive the optimal lockdown policy subject to the ICU constraint just like Loertscher and Muir. The real *tour de force* of the paper is to manage to find an analytical solution to the latter problem (Loertscher and Muir's results being essentially based on numerical solutions). Just like Loertscher and Muir, Miclo and co-authors question the common wisdom of the "flattening the curve" strategy with continuous lockdown from the start of the epidemic. Instead, the optimal policy should be discontinuous. As in Loertscher and Muir, the epidemic should be left unregulated in a first phase and when the ICU constraint is approaching society should quickly lock down, which yields the discontinuity in optimal policy mentioned above. After the lockdown, regulation should gradually be lifted, again as in Loertscher and Muir.

 $<sup>^{26}</sup>$ Bonneuil (2021) is another contribution dealing with ICU capacity constraint. However, the framing is quite different. Bonneuil is more concerned with the optimal management of priority access to ventilators. Using the theory of queuing processes, he proposes age and sex-based priority criteria derived from the minimization of the mean mortality rate weighted by age- and sex-specific life expectancies.

 $<sup>^{27}</sup>$ Clearly, this setting generalizes the age-dependent lockdown policies studied by Gollier (2020) for example.

**Covid and the macroeconomy** We shall more briefly present some of the *JME* contributions to the study of Covid macroeconomic impact, in particular the distributional and financial. The reader is referred to Augeraud-Véron et al. (2021) and Desbordes (2021) for more interdisciplinary explorations, the former devoted to the theoretical analysis of the link between zoonotic disease risks and the actual biodiversity loss trend (with the resulting implications in terms of risk-reducing and mitigation policies, including conservation biodiversity instruments), and the latter studying the geographic drivers of disease outbreaks in connection with climate disruptions.

#### Economic consequences of lockdown

The significant impact of habits on our consumption patterns has been well-established in both psychological and economic literature. The COVID-19 pandemic, marked by social distancing measures and lockdowns, brought about a profound transformation in our daily routines. A large literature has explored the repercussions of these restrictive measures on particular habits. There is substantial evidence indicating the reinforcement of certain habits, such as increased reliance on online shopping and streaming services, alongside the weakening of others. Therefore, this prompts a broader investigation into how shifts in habits during a lockdown could influence post-pandemic consumption behavior and the overall economy. Within the framework of a two-sector infinite horizon economy, Bambi et al. (2024) shows that the demand for products originating from the sector subject to the lockdown could either contract or expand compared to pre-pandemic levels, depending on the duration of the lockdown and the resilience of consumer habits. They further point out that the end of a lockdown may be characterized by a price surge due to a combination of strong demand of both goods and rigidities in production.

#### Distributional consequences of epidemics

The impact of epidemics on inequalities and poverty is quite well treated in economics, including economic theory as outlined before. The COVID-19 is currently generating a vivid debate on these essential questions as multiple (new) sources of concern about widening inequalities have emerged in the course of the health crisis, ranging from the unequal welfare consequences of global lockdown policies to unequal access to teleworking through the current tough international battle in the vaccines market. Indeed as outlined by Atolia et al. (2021) in the *JME* Covid special issue, the distributional consequences of the pandemic may be even more severe and far more long-lasting than its growth and productivity impacts.

Atolia et al. (2021) provide with a careful quantitative assessment of the distributional consequences of COVID-19 using a full-fledged general equilibrium model with heterogeneous agents. The primitive endogenous distributional mechanism relies on the relationship between the agents' relative wealth and their respective allocation of time between work and leisure. This mechanism is active when the economy has to respond to external shocks, including epidemic shocks and the inherent (adverse) productivity shocks. Furthermore, Atolia et al. (2021) embed this primary mechanism into a two-sector Ramsey model of health to capture some more refined elements of the COVID-19 epidemic.

In this context, the interaction between the speed with which the economy reopens and the spread of the virus will determine the post-COVID-19 steady state's nature. Indeed, the interaction between the spread of the infection and the speed of opening up the economy may have long-run aggregate effects, as well as permanent distributional effects, depending upon the chosen speed. The paper's key result is that less developed economies are likely to suffer more permanent distributional effects given their infrastructure disadvantage leading to delayed reopening. As importantly noted by the authors, much of the debate among policymakers attributes the increase in income inequality following the COVID-19 experience to small firms and businesses, temporarily closed during the pandemic, and being unable to recover. The main contribution of Atolia et al. (2021) is to identify a deeper and more specific channel: the long-run inequality generated derives from the intrinsic dynamics of the economy as it transitions in the process of re-opening in the face of a strong transitory epidemic shock.

#### Covid impact on financial markets

Despite the declines in GDP and consumption, asset prices, including stock prices, have continued to rise during the resultant economic crisis. This contrasts with the decline in asset prices that typically accompanies a recession. During the Great Depression, stocks lost about three quarters of their value from their peak in late 1929 to their trough in 1932. By 1936, they had recovered only about half of those losses. In his contribution, Herrenbrueck (2021) notes that the Covid experience is very different. The Down Jones Industrial Average lost about 40% of its value from the end of February to the end of March 2020. However, half of those losses had been recovered by late May, and the index closed the year 4% higher than the peak value of February 13. What are the mechanisms leading to this singular impact of an epidemic-led recession on the financial markets? Herrenbrueck uses an elementary formal model, a one-agent, discrete time economy where a longlived asset is traded in every period. If  $\lambda$ , q and r denote, respectively, the current values of marginal utility of income of the agent, the price of the asset and its return, the following fundamental equation must hold:

$$\lambda q = \rho \; \lambda^e (q^e + r^e),$$

where  $\rho$  is the time discount factor and  $x^e$  is the future (expected) value of x. Herrenbrueck submits that the type of shock resulting from a pandemic imposes an upper bound on the agent's consumption. The marginal utility of income during the pandemic is lower  $(\lambda < \lambda^e)$  and if this were to be the permanent state of the economy asset prices should drop  $(q < q^e)$ . But, following the fundamental equation above, he shows that the price may indeed go up if the pandemic is assumed to be short enough. The reason is that the lower marginal utility of income during the pandemic makes the agent value her future consumption relatively more, so her demand for the asset increases. Remarkably, the agent's marginal utility of income drops, although her income is lower, because of the bound on consumption.<sup>28</sup>

<sup>&</sup>lt;sup>28</sup>More complete theories on these Covid stock market dynamics have been elaborated since Herrenbrueck's initial impulse. A rigorous contribution is due to Morimoto and Suzkuki (2022) who use an asset pricing model of a multisector production economy (including pandemic disaster) under ambiguity. They show that two features of the pandemic, namely ambiguity and sector-specific shocks, are critical determinants of the unusual asset price dynamics observed.

## 5 Covid-19 epi-econ literature: Microeconomics and economic behavior

Understanding microeconomic and behavioral dimensions is especially crucial, as it examines how individuals respond to strategic elements and incentives stemming from their social interactions during an epidemic. The epi-econ literature deals with this discourse by incorporating perspectives from game theory, behavioral economics, and network theory into the modeling of a pandemic. It offers a nuanced understanding of the complex dynamics at play during an epidemic, shedding light on the strategic considerations and behavioral patterns that influence the spread and management of a pandemic. In this subsection, we examine several papers published in *JME* that effectively integrate aspects of microeconomics, behavioral economics and network theory into the exploration of pandemics. A key concern during the pandemic was to what extent is the change in behavior due to NPIs and to what extent due to individual response to the situation. This is an area where epi-econ modelling is an important way to frame and analyze the issues.

Incentives for self-isolation In the time of pandemic, incentives for self-isolation emerge as individuals consider stepping outside for social interactions. The uncertainty regarding their infection status and the potential for reciprocal transmission prompts a cautious approach. Confronted with the looming threat of contagion, individuals naturally seek ways to reduce the risk of contracting the virus. One may choose to abstain from visiting the other entirely, or if the interaction is deemed essential, precautions like wearing a mask might be adopted. The decisions undertaken by each person in this scenario raise questions about their economic well-being, the associated infection risks, and the trade-offs between costs and benefits. Additionally, the socioeconomic distribution within the community plays a pivotal role in shaping the infection risks they encounter.

These points are carefully examined in Bhattacharya et al. (2021), offering a parsimonious, rational-choice static model. In the model, There are three groups of agents. One group is showing symptoms and entering strict quarantine as symptomatic and infected (SI), and the other two groups are either asymptomatic and infected (AI) or asymptomatic and uninfected (healthy, AH). As the period starts, people know if they are in the SI pool or not. What they do not know is whether they are in the AI or the AH pools. Such people face two extensive-margin decisions: the decision to socialize, which brings joy but may raise the infection risk, and the decision to engage in prevention, which brings utility losses but reduces the chance of infection. Moreover, agents are heterogeneous in their endowment (income). Agents under rational expectations take the masses of the three groups, SI, AH, and AI, as given. An individual determines her infection risk, and in turn, her going-out and protection choices, based both on these masses and her position on the endowment distribution. Bhattacharya et al. (2021) find that a mean-preserving increase in pre-existing income inequality unambiguously increases the equilibrium proportion of unprotected, socializing agents and may increase or decrease the proportion who self-quarantine. Strikingly, while higher pre-COVID inequality may or may not raise the overall risk of infection, it increases the risk of disease in social interactions.

Similarly, Baril-Tremblay et al. (2021) analyze the spread of an infectious disease in a population when individuals strategically choose how much time to interact with others. The population consists of two types: sympomatic and asymptomatic. In the absence of symptoms, individuals are uncertain about their type and continually weigh the costs and benefits of self-isolation based on their perceived likelihood of being infected. They show that all equilibria of the game involve social interaction, and characterize the unique equilibrium in which individuals partially self-isolate at each date. They apply the model to policy analysis showing that governments gain no advantage in delaying announcement that the pandemic is imminent and that mitigating policies meant to flatten the epidemic curve may not be effective at doing so even when they avert deaths.

**Information and antibody testing** During a pandemic, information plays a pivotal role in decision-making. Antibody testing, as a non-pharmaceutical intervention, introduces a valuable element of information by revealing individuals' immune status to the virus. This not only aids in understanding the prevalence of past infections, but also plays a crucial role in averting the escalation of contagion. From a microeconomic standpoint, this information influences individual choices regarding risk perception, healthcare decisions, and social interactions. The accessibility and accuracy of antibody testing impact market behaviors, healthcare resource allocation, and contribute to the broader public health strategy aimed at mitigating the impact of the pandemic.

Guimarães (2021) uses a parsimonious compartmental SEIRD model, in which individuals' optimal social activity depends on their health state and uncertainty. In a world with perfect information, susceptible agents would constrain social activity to reduce exposure to the virus, while recovered agents would not. But, under health state uncertainty, agents rely on expectations of their health state to choose social activity: recovered agents may restrain themselves excessively while, crucial for contagion, susceptible and asymptomatic agents may be excessively active. In the model, they find that optimal behavior critically depends on access to antibody tests. As the probability of being immune builds up, susceptible and asymptomatic agents without access to antibody tests become more active than those with access because the former agents think they might be immune whereas the latter know that they are not. Therefore, increasing the scale of antibody testing lowers social activity and contagion by raising the share of agents that are sure of not being immune. In the context of the COVID-19 pandemic, more than half of the infected are asymptomatic. Calibration of the model to UK data shows sizable welfare gains -12% of COVID-19 related deaths averted from making antibody tests widely available.

**Uncertainty and policy interventions** In the face of a novel or rapidly evolving health crisis, such as a pandemic, the uncertainty surrounding the severity of a disease poses a considerable challenge for governments when determining the optimal timing for implementing lockdown measures. Balancing the need to protect public health with the desire to minimize economic and societal disruptions becomes particularly intricate. Governments must carefully weigh available data, consult with experts, and consider the potential consequences of delayed or premature lockdowns.

Bandyopadhyay et al. (2021) delve into this research question. They analyze a threeperiod model where the government has to decide whether to impose a lockdown in a country to prevent the spread of a possibly virulent disease. If the government decides to impose a lockdown, it has to determine its intensity, timing and duration. They find that there are two competing effects that push the decision in opposite directions. An early lockdown is beneficial not only to slow down the spread of the disease, but creates beneficial habit formation, such as social distancing, developing hygienic habits, that persists even after the lockdown is lifted. Against this benefit of an early lockdown, there is a cost from loss of information about the virulence and spread of the disease in the population in addition to a direct cost to the economy. Given the information in any period that the disease is virulent, they analyze whether the government should impose a lockdown, how intense should the lockdown be and if imposed early, for how long should it be. Furthemore, they examine the cutoff probability that the disease is virulent at which a government decides to lockdown and how this shifts over time as a function of the accuracy of the signal each period, the strength of the behavioral response, the cost to the economy, the magnitude of the backlash effect and the expected time of arrival of a vaccine/treatment.

**Modelling disease transmission** Modelling the spread of infectious diseases and understanding the intricate linkage between disease transmission and economic activity is crucial. It is often assumed that infections spread through random interactions within the population. However, it is essential to recognize that the dynamics of whom we interact with and how those interactions occur are intricately influenced by our economic and social lives. These factors play a significant role in shaping the patterns of disease transmission and impact the broader outcomes studied in the epidemic-economic literature. While this is recognized in the epidemiology literature<sup>29</sup> modelling in the econ-epi literature is more limited.

Based on the theory of random matching, Camera and Gioffré (2021) models explicitly how epidemics spread through economic activity. The model economy has a constant population composed of individuals who can earn income only in periods in which they meet a trade partner. Meetings occur on a market where a matching process pairs individuals at random. The model assumes transmissibility via asymptomatic individuals. This implies that individuals who are unaware of being infected, have no incentive to stay out of the market and, hence, can spread the disease by meeting healthy trade partners. Repeating this random matching process period after period is how the epidemic spreads over time, which is tied with economic activity. They construct transition matrices, and then calculate the dynamic evolution of the epidemic when lockdowns of various degree of severity are imposed. Numerical analysis suggests that a lockdown is generally welfare-enhancing if the infection spreads easily. However, the welfare benefit rapidly dissipates as the lockdown length increases, and turns into a welfare loss eventually.

Use a network framework, Bouveret and Mandel (2021) studies the containment of epidemic spreading and the role of social interactions. In their model, each individual has the option to invest in the network, thereby reducing the speed of contagion, which benefits all individuals connected to them. The magnitude of this external effect depends on the specific connectivity between each pair and thus on the structure of the network. They characterize

<sup>&</sup>lt;sup>29</sup>See Keeling and Rohani (2008) for example.

individually rational and socially efficient behaviours using the notions of communicability and exponential centrality, and then derive a quantitative measure of the inefficiency induced by individual behaviours. Their findings not only underscore the potential extreme inefficiency of individual actions in limiting epidemic propagation but also highlight the prospect of designing effective containment policies taking into account the network structure.<sup>30</sup>

### 6 Covid-19 epi-econ literature: Mathematical advances

As outlined earlier, epi-econ models have a complex structure as they build on non-concave state equations which embedded in optimal control settings, can lead to analytically intractable optimality explorations. Existence of a solution is also not immediate. The introduction of disease related mortality poses yet another challenge as keeping track of the changing population size adds a new state variable which affects discounting and unlike the existing literature it is non-convex in state and control variables. Another problem, not specific to the Covid modelling, concerns the modelling of uncertainty, be it radical or not. The Covid case made the search for appropriate stochastic extensions, methods and policy recommendations even more urgent than before as scientists are anticipating the emergence of more pathogens in the next years possibly leading to periods of uncertainty as acute as in the Covid crisis. We summarize here below the contributions of a few *JME* articles and related papers along these two research lines, dealing with deterministic models concerning optimality, existence, and discounting and the modelling uncertainty, respectively.

**Deterministic Models** Beside the non-concavities which come from the specifications of the epidemiological differential equations, several other departures from concavity can also show up in other specifications of the epi-econ models, starting with the objective functions.<sup>31</sup> The discussion is done under the three issues of existence, population dynamics, and optimality (sufficiency)

Existence Due to the non-concave and non-monotonic laws of motion of the state variables results for the existence of a solution do not apply in these models. (Goenka et al., 2014) show the existence of an optimal solution by showing that the control variable weakly converge in the weak topology  $\sigma(L^1(e^{-\theta t}), L^{\infty})$ , while the state variables converge pointwise. The problem is that even if there is a weakly convergent sequence, the limit point may not be feasible. For pointwise convergent sequences, the continuity is all that is necessary to prove the feasibility. Therefore, concavity is not needed for state variables. They show that limit point is indeed optimal in the original problem. For weakly convergent sequence, Mazur's Lemma is used to change into pointwise convergence. Jensen's inequality is used to eliminate the convex-combination-coefficients to prove the feasibility. Thus, concavity with respect to control variables is crucial. Calvia et al. (2023) use a dynamic programming

 $<sup>^{30}</sup>$ Acemoglu et al. (2023) models social activity and voluntary distancing as a network formation problem and use a simple percolation process to represent the spread of a virus over the endogenous social network. The focus of their investigation centers on the impact of testing policy on voluntary social distancing and the spread of an infection.

<sup>&</sup>lt;sup>31</sup>See Calvia et al. (2023) for a deeper account of these "singularities".

approach to analyse situations when concavity of the objective function can fail.

Disease related mortality and endogenous discounting: With disease related mortality there is an endogenous change from in population size change. The epi-econ literature has taken two different ways to account for the changing size of the population. One following Eichenbaum et al. (2021) keeps the the number of economic agents fixed but those who die enter into a holding state where they do not consumer or produce. The second approach is to weight the per-capita utility by population size. Without disease related mortality, the population grows at rate  $(b - d) \ge 0$  so the discount rate  $\rho$  increases by this amount. When there is disease related mortality, the change in population is endogenous and following Uzawa (1968), d'Albis and Augeraud-Véron (2021), Goenka et al. (2021) and Goenka et al. (2024a) note that it makes the discount rate endogenous. There is a new state variable of the endogenous discount rate,  $\Lambda = \rho + (b - d) + \delta i_i$ , the last term is the disease related mortality. In this formulations the effect of disease related mortality on discounting becomes clear. As the equilibrium shadow prices depend on  $\Lambda$  the effect of increasing mortality on affecting inter-temporal choices can be traced out.

Sufficiency/Optimality: All these complications make the optimal control epi-econ problems very delicate to tackle. Optimality of the Pontryagin first-order conditions is very far from granted. Most of the epi-econ papers of this stream use computational methods to identify optimal paths, which is not less delicate as the non-concave features of these models also generate multiple optimal regimes, Skiba points and the like (see Caulkins et al. (2021), again). Often in these cases, optimality is checked with *ad hoc* numerical procedures. In some specific cases, analytical exploration of optimality (or sufficiency of first-order conditions) is however possible. But no standard tool can be invoked even in such cases. Two general avenues can be taken.

<u>Hamiltonian-based methods</u>: Interesting work has been performed by Goenka, Liu, and Nguyen using Hamiltonian-based methods. As noticed by (Gersovitz and Hammer, 2004) and (Goldman and Lightwood, 2002), Goenka et al. (2014) show that control problem does not satisfy either the Arrow or Mangasarian sufficiency conditions. The maximized Hamiltonian,  $H^*$ , need not be concave as it can be the case that  $\frac{\partial^2 H^*}{\partial^2 l} > 0$ . They tackle the problem of sufficiency of the first order conditions to the control problem by showing directly the optimality conditions in Leitmann and Stalford (1971) hold. The Leitmann-Stalford theorem is a powerful result but has not been used much in the economics literature as the conditions are difficult to verify. It can however be applied for example to growth model proposed by Goenka et al. (2014), already developed in Section 3. To use the Leitmann and Stalford conditions in this context, they show that  $\{c, m\}$ , the control variables, are bounded, and the state vector  $x = \{l, k, h\} \in L^1(e^{-\theta t})$ . This implies that the co-state variables lie in  $L^1(e^{-\theta t})$ . This yields  $\lim_{t\to\infty} e^{-\theta t} \langle \lambda, x^*(t) - x(t) \rangle = 0$  (Leitmann and Stalford require it to be less than or equal to zero). This is crucial as when to check the maximality of the Hamiltonian it can decomposed into two parts: the first just relies on the control variables and we have concavity in the objective function in control variables, and thus, using standard results the difference between the candidate solution and any other solution is non-negative; and a term that depends on the co-state and the state variables as given above. Recall, the non-concavity in the problem arises from the law of evolution of l only. As this term converges to zero, they are able to obtain sufficiency of the first order conditions. Thus, three things turn out to be important in this problem: the boundedness of the state and control and hence, co-state variables; concavity of objective in control variables; and the ability to separate the control and state/co-state variables in the Hamiltonian. Other applications of the Leitmann-Stalford theorem, rely on special structures such as convexity (Feichtinger et al. (2010)) which is violated in our case. The direct approach using Leitmann and Stalford (1971) conditions are used by Goenka et al. (2021) to show sufficiency in a similar model with *SIR* dynamics with disease related mortality, and in (Goenka et al., 2024a) for *SIRS* dynamics with disease related mortality. In these two papers the state variable  $\Lambda$  behaves in a non-monotonic and non-concave manner due to the evolution of current infections, and thus, existing results for endogenous discounting models are not applicable requiring new results.

<u>Dynamic programming-based methods</u>: A natural alternative to addressing optimality issues is dynamic programming which need not full concavity to be operational via the solution of HJB equations. This approach has been followed by Fabbri et al. (2021) to tackle an optimal control version of the age-structured 1927 Kermack-McKendrick model. As any age-structured model in continuous time is infinite-dimensional, so is the resulting optimal control problem. The technique proposed is a dynamic programming method first designed by Bensoussan et al. (2007) for infinite-dimensional control problems. Fabbri et al. (2021) is the first paper to establish a verification theorem in the epidemic control framework to the best of our knowledge. Indeed, the paper provides a sufficient condition for optimality in terms of the value function and its derivatives.

More recently, Calvia et al. (2023) use dynamic programming to solve a generalized version of the Alvarez et al. (2021) model. They prove some continuity properties of the value function of the associated optimization problem and they study the corresponding HJB equation, ultimately proving that the value function solves it (in the viscosity sense). They later discuss to which extent and under which conditions some optimality conditions can be obtained. To our knowledge, this work is the first contribution towards a complete analysis of non-convex dynamic optimization problems using dynamic programming. It can open therefore the door to a better appraisal of optimality issues in the analysis of optimal control epi-econ models.

**Dealing with uncertainty** The Covid crisis has evidenced the lack of stochastic frames to better account for uncertainty particularly in the first phase of outbreaks. In this early phase of the Covid crisis, most of the epidemic control policies have been undertaken under strong uncertainty: even the biological drivers of this emerging disease were not very well understood in the first months, not speaking about the main infection channels which remain unclear for a while. The emergence of the virus variants has made the story even more intricate in this respect. A lot remains to be done in this area of epi-econ research, which has indeed become very active in the last months (see Boucekkine and Loch-Temzelides (2024) for a brief report).

A first *JME* contribution to this line of research is due to Federico and Ferrari (2021)

who examine the optimal lockdown problem under a stochastic SIR infection dynamics. Basically, they assume that the infection rate of their SIR model (that's parameter  $\beta$  in the Caulkins et al. (2021) model seen in Section 4) is stochastic, following a diffusion process. While the process trend can be affected by an epidemic policy, the epidemic diffusion has a noise (precisely, a Wiener process) to capture all factors not anticipated or not controllable by the planner. A key aspect in the modeling is that the epidemic transmission rate is a state variable, which tracks more closely how actual epidemic control has been taking place during the current COVID-19 crisis. Federico and Ferrari also provide a full mathematical characterization of the control problem and derive, through several numerical exercises, its most important practical implications in terms of optimal lockdown.

A more recent *JME* contribution, due to Sun and Zhao (2023), takes more seriously the nature of uncertainty under Covid. More precisely the authors study the government's optimal decision-making facing an outbreak under uncertainty, a sizeable uncertainty to the point that the government only follows its own perceived belief. Indeed, both the government and households update their beliefs regarding the pandemic through Bayesian learning processes, but in this framework, the government makes decisions based on their own beliefs. While this limits the strategic interactions between the two players, this corresponds to a number of actual situations in Covid times, at least in the early phase of the disease where the governments were definitely taking the lead (presumably based on a surperior set of information). The authors derive a number of interesting results on the optimal timing of lockdowns in such a frame. In particular, they prove that the government should implement a lockdown to stop the virus spread when the perceived policy effect on the infection rate is below a certain threshold, the latter being a complex function of the net health gains from the policy change, uncertainty, and household health service concerns. This, according to Sun and Zhao, allows to respond at least partially to the recurrent questions on why certain national governments have implemented a lockdown, why others have not, and why populations' responses to these policies (or absence of policies) have been so diverse.

### 7 Areas for further investigation

The Covid-19 crisis led to a rapid assimilation of techniques from epidemiology modelling into economics. Given that there were no clear preventive or therapeutic medical strategies, the onus was on NPIs to control the pandemic. The initial hope was that the introduction of vaccines would end the pandemic. Thus, a lot of the initial work as also reflected in the *JME* Special Issue was on the optimal NPI strategy, usually a lockdown as these were being discussed and adopted in many OECD economies.

**Greater disaggregation** The epi-econ models differ from epidemiological models not only because they include economic variables, but also they are largely control models. Due to the curse of dimensionality and to be able to parse out clear implications they have been parsimonious - with one or atmost two age groups, homogeneous random mixing, often a single production sector and often without capital dynamics. From a policy perspective, this is restrictive as they are not detailed enough to answer questions such as whether to have a targeted lockdown or a general lockdown, which age groups or occupations to restrict if at all, whether to shut down schools,<sup>32</sup> etc. Policy makers tended to follow epidemiology modelling in setting NPI policy which are far more disaggregated as they do not solve a control problem but simulate scenarios.<sup>33</sup> Even though there was a great concern for distributional effects and the question of trade-off between health and wealth, epi-econ modelling was not used in practice by almost all OECD economies.<sup>34</sup>

The way forward will require consideration of more disaggregated models so that they could inform policy making. The modelling of heterogeneities - age, occupation, industries, spatial - needs further investigation. Haw et al. (2022) is a first step in this direction. To model the economy it uses an input-output framework without capital. There is scope for generalisation moving away from the special assumptions. Network structure modelling to study interpersonal interactions, as well as supply chains (domestic and international) need to be integrated into epi-econ models.

To go beyond a few different types of agents, and allow for greater individual heterogeneities which we know have been important such as wealth, productivity, human capital, age, location, etc., a heterogeneous agent models or mean-field games approach could be developed. Ghilli et al. (2023) and Goenka et al. (2024b) are two papers using epi-econ mean field games. The first paper studies human capital and the second health and economic (income and wealth) distributional issues.

Long run effects The hope of the Covid-19 pandemic being short-lived has not materialised. While its outbreak focussed attention to how to control a new pandemic there is also a need for studying long-run effects of epidemics. The modelling of investment and human capital and long-run effects that were the main concerns of the pre-pandemic literature <sup>35</sup> are likely to gain prominence. The modelling of technological change in response to the pandemics and WFH in an epi-econ framework and its growth effects remains to be done. School closures were a contentious topic not only because of short-run effects on children and parental responsibility but also because of long run effects on human capital accumulation and inter-generational disparities. As the Covid-19 pandemic seems to have been become endemic , will the long-run effects be similar or not to other infectious diseases? There is a need to study these longer run effects of pandemics.

The asymmetric health effects on different population groups and effects on economic inequality was a key concern during the recent pandemic. The long-term distributional effects within and across generations still needs to be fully understood. (Atolia et al., 2021) was an early paper, but the full effects on health and economic inequality is an emerging topic. (Goenka et al., 2024b) study the consequences of optimal protective and preventive measures in a heterogeneous agent continuous time framework (Achdou et al. (2022)). They show how optimal preventive and treatment choices by individuals can increase existing wealth

 $<sup>^{32}</sup>$ Chernozhukov et al. (2021) addressed this empirically.

 $<sup>^{33}</sup>$ See for example, Ferguson et al. (2020) which guided initial UK response and ? for the later part of pandemic.

<sup>&</sup>lt;sup>34</sup>This is based on Goenka's two year participation in the International Best Practices Group formed by Cabinet Office and the Foreign, Commonwealth, and Development Office to inform UK government on Covid policy. See also Patoulliard and et al. (2024).

<sup>&</sup>lt;sup>35</sup>See (Goenka et al., 2014), (Goenka and Liu, 2020), (Goenka et al., 2021), (Goenka et al., 2024a)).

inequality as the elasticity of these choices are increasing in wealth. <sup>36</sup> In the stationary equilibrium, the wealthier have better health outcomes of lower infections. The insight that the wealthier with larger assets have better health outcomes in a fully integrated epi-econ framework also holds in representative agent frameworks.<sup>37</sup>. However, the heterogeneous agent framework allows for a richer discussion of economic policy interventions.

**Mental health** A very important and novel research avenue has emerged in the course of the Covid-19 crisis, related to the use of NPIs at an unprecedented scale. With obvious intersections with the inequality channel commented above, the **mental health** problem triggered by the intensive and relatively long lockdown episods in 2020 and 2021 has become one of the intriguing singularities of this health crisis, and as such, it has been explored in a number of studies, mostly under way. Very few theoretical analyses have been devoted to this topic so far. When it's alluded to, it's represented in an overwhelmingly metaphorical way. For example, Caulkins et al. (2021) includes a lockdown fatigue component, which is endogenous, but not microfounded.

An early microfoundation of this channel has been very recently proposed by Adda et al. (2024) in a context where, like in the French case, individuals adjust their mobility decisions sequentially in response to policy moves regarding the parameters of the lockdown.<sup>38</sup> Define  $d^*$  the desired travel distance in the absence of the epidemic for a given individual (we skip here individual heterogenity). During the epidemic, individuals have to reduce their mobility either for fear of being fined when a lockdown is underway or for fear of contamination. Denote by the m the actual stock of cumulative missed distance since the start of the epidemic. If the individual decides to walk an additional distance d in current period, this stock evolves as follows:

$$m' = (1 - \delta)m + \frac{d^* - a}{d^*}$$

where m' is the next period stock of missed distance, and  $\delta$  is the depreciation rate of this stock. This missed stock determines the long-term mental health, h of an individual, together with short-run mobility restrictions following the following specification:

$$h = \alpha \ (1 + (d^* - d))^{\alpha_{SR}} \ m^{\alpha_{LR}} \ (1 + I)^{\alpha_I},$$

where I is the period infection rate, and  $\alpha_>0$ . Mental health is therefore a function of restricted mobility's short- and long-run effects, plus additional psychological effects induced by the severity of the infection and the quality of the confronted health system. If  $\alpha_{SR}$  is different from zero, then an imposed lockdown affects mental health contemporaneously. If  $\alpha_I > 0$ , the higher the prevalence, the worse its impact on mental health. This is to capture especially the earlier phases of the pandemic, when no vaccines and few face masks were available. The individuals choose their optimal mobility per period integrating the mental health component in their utility function. The stricter the mobility constraints imposed by the government, the more likely the latter component will lead the individuals to not fully

 $<sup>^{36}</sup>$ Glover et al. (2023) study similar questions in a economy with three types of agents.

<sup>&</sup>lt;sup>37</sup>See (Goenka et al., 2014), (Goenka and Liu, 2020), (Goenka et al., 2021).

 $<sup>^{38}</sup>$ Adda et al. (2024) estimate their model using French mobile phone companies data, and then use the estimated model for policy counterfactuals studies.

comply with these constraints despite the risk to be fined and the larger probability to be contaminated. Not surprisingly, the individuals will more easily overlook the contamination risk as public trust (in the efficiency of lockdown) is not large enough. This aspects is also considered in Adda et al. (2024): individuals learn about the efficiency of lockdowns along the way (Bayesian learning), the interplay between mental health dynamics and public trust being the central part of the model.

**Modelling approaches** As discussed above, the use of mean-field games for epi-econ modelling can be further developed. Proving analytical results in economic mean field games except in special frameworks can be challenging (Achdou et al. (2014)) so numerical methods may be the way forward.

The existing epi-econ literature has tended to use Hamiltonians to solve the control problems in epi-econ models. The technical issues that arise with these have been discussed above and should be seriously considered. The dynamic programming approach while promising but is not without its own challenges (Calvia et al. (2023)). The advantage of this approach is that it gives a policy function rather than a time-path as in the Hamiltonian approach. From a policy perspective, many governments<sup>39</sup> followed a "dash-board" approach following a set of indicators and taking decisions based on how these change. This is nothing but having state-contingent policy functions. Thus, using continuous time dynamic programming (HJB approach) should become more salient. (Goenka et al., 2024c) study how policy functions are effected by the choice of the epidemiology model. If one compares the value functions across the SIR and SIRS model, they look qualitatively similar but the policy functions and equilibrium dynamics look very different.

As mentioned earlier, the epi-econ literature has tended to use deterministic epidemiology models. The emergence of new viruses such as the SARS-Cov-2 as well us its mutation suggests that there is uncertainty about the nature of the epidemiology dynamics. There is potential for both using stochastic epidemiology modelling, as well as thinking seriously about Knightian uncertainty and ambiguity. (?) is one of the few papers that incorporates insights from the literature of ambiguity aversion and model uncertainty in the design of lockdown policy. This may be a useful framework to model resilience to emerging pandemics.

**Conclusion** The Covid-19 crisis has raised numerous research questions which are relevant for economic theory and mathematical economics. This article has outlined the important role played by the *JME* in mathematical economic epidemiology modelling. No doubt that it will remain a leading outlet in this highly involved technical area.

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<sup>&</sup>lt;sup>39</sup>At least the U.K. government, and what one can infer, many European countries.

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