UCLouvain

## linma1691

2023

## Discrete mathematics - Graph theory and algorithms

| 5.00 credits | 30.0 h + 22.5 h | Q1 |
|--------------|-----------------|----|
|              |                 |    |

| Teacher(s)           | Blondel Vincent ;Delvenne Jean-Charles ;   |  |  |  |  |
|----------------------|--|--|--|--|--|
| Language :           | French   |  |  |  |  |
| Place of the course  | Louvain-la-Neuve   |  |  |  |  |
| Prerequisites        | This courses assumes that the elementary notions of discrete mathematics are acquired such as taught in LEPL1108.  |  |  |  |  |
| Main themes          | Introduction to the language and theory of graphs: questions of characterization, isomorphism, existence and enumeration. Properties of directed and undirected graphs such as connectivity, planarity, k-colorability and the property of being Eulerian, perfect, etc. Modelling of practical problems: data structures and algorithms for the exploration of graphs. Basic graph algorithms and an analysis of their complexity.  |  |  |  |  |
| Learning outcomes    | At the end of this learning unit, the student is able to :   |  |  |  |  |
|                      | AA1 : 1,2,3  More precisely, by the end of the course the student will be able to :  |  |  |  |  |
|                      |  |  |  |  |  |
|                      | *model various problems in the language of graph theory     *identify if a graph-theoretic problem has a known efficent algorithmic solution or not     *propose and apply an algorithm to solve sucha a problem, at least for some classes of graphs     *prove in a clear and rigorous fashion elementary properties related to the concepts covered in the course   |  |  |  |  |
|                      |  |  |  |  |  |
| Evaluation methods   | The students are evaluated through assignments during the semester and through a written (or possibly oral depending on the circumstances) exam, based on the specific objectives described above. The semester assignments amount to 25% of the final grade (in January and in August). There is no opportunity to re-make assignments outside the semester.  |  |  |  |  |
|                      | These assignments lead to a unique grade, given after the last assignment. Failure to respect the guidelines explained on Moodle, in particular regarding the use of online resources and/or collaboration between students, for any assignment may lead to a zero grade for the whole assignment grade.   |  |  |  |  |
| Teaching methods     | The course is organised in lessons and supervised exercise sessions.   |  |  |  |  |
| Content              | Structure and characterisation of graphs - basic concepts - degree, connected components, path, cycle, cut, minor, etc. Exploration of graphs and tests of their properties - k-connectedness, Eulerian graphs, planar graphs, etc. Flows - theorems of Menger and Hall, maximum flow and minimum cost flow algorithms and their complexity. Problems: finding optimal matchings and stable sets, the travelling salesman problem, cut, graph partitioning and graph colouring problems. Separation between "easy" and "hard" problems, NP-completeness. |  |  |  |  |
| Inline resources     | Moodle page of the course  |  |  |  |  |
| Dilli I              | Ouvrage de base (non obligatoire) / primary (non mandatory) reference :  |  |  |  |  |
| Bibliography         | Graph Theory with Applications, A. Bondy- U.S.R. Murty, Springer, téléchargement libre/free download  Aussi /also:   |  |  |  |  |
|                      | <ul> <li>Algorithmic Graph Theory, Alan Gibbons, Cambridge University Press 1985</li> <li>Introduction to Graph Theory, Douglas West, Prentice Hall 1996.</li> <li>Combinatorial Optimization, W.R. Cook et al., Wiley 1998.</li> <li>Network Flows, Ahuja et al., Prentice Hall 1993.</li> </ul>  |  |  |  |  |
| Faculty or entity in | MAP  |  |  |  |  |
| charge               |  |  |  |  |  |

| Programmes containing this learning unit (UE)       |          |         |              |                   |  |  |
|---|----------|---------|--------------|-------------------|--|--|
| Program title                                       | Acronym  | Credits | Prerequisite | Learning outcomes |  |  |
| Additionnal module in Mathematics                   | APPMATH  | 5       |              | ٩                 |  |  |
| Minor in Applied Mathematics                        | LMINOMAP | 5       |              | ٩                 |  |  |
| Specialization track in Applied Mathematics         | FILMAP   | 5       |              | ٩                 |  |  |
| Master [120] in Electrical<br>Engineering           | ELEC2M   | 5       |              | ٩                 |  |  |
| Master [120] in Computer<br>Science and Engineering | INFO2M   | 5       |              | ٩                 |  |  |
| Master [120] in Computer<br>Science                 | SINF2M   | 5       |              | ٩                 |  |  |
| Mineure Polytechnique                               | MINPOLY  | 5       |              | ٩                 |  |  |