

5 credits

30.0 h + 15.0 h

Q1

Teacher(s)	Haine Luc ;
Language :	French
Place of the course	Louvain-la-Neuve
Main themes	Elliptic functions of Weierstrass and Jacobi, associated elliptic curves, Abel's theorem, addition theorem, selected applications in geometry, mechanics and number theory.
Aims	<p>Contribution of the course to learning outcomes in the Bachelor in Mathematics programme. By the end of this activity, students will have made progress in:</p> <ul style="list-style-type: none"> - Recognise and understand a basic foundation of mathematics. In particular: <ul style="list-style-type: none"> -- Choose and use the basic tools of calculation to solve mathematical problems. -- Recognise the fundamental concepts of important current mathematical theories. -- Establish the main connections between these theories, analyse them and explain them through the use of examples. - Identify, by use of the abstract and experimental approach specific to the exact sciences, the unifying features of different situations and experiments in mathematics or in closely related fields. - Show evidence of abstract thinking and of critical spirit. In particular; <ul style="list-style-type: none"> -- Argue within the context of the axiomatic method. 1 -- Recognise the key arguments and the structure of a proof. -- Construct and draw a proof independently. -- Evaluate the rigour of a mathematical or logical argument and identify any possible flaws in it. - Be clear, precise and rigorous in communicating. <ul style="list-style-type: none"> -- Write a mathematical text in French according to the conventions of the discipline. -- Structure an oral presentation in French, highlight key elements, identify techniques and concepts and adapt the presentation to the listeners' level of understanding. <p>Learning outcomes specific to the course. By the end of this activity, students will be able to:</p> <ul style="list-style-type: none"> - Construct holomorphic and meromorphic functions in terms of infinite series or products. - Apply Abel's theorem and the addition theorem of elliptic functions theory in various contexts. - Solve problems which use elliptic functions and elliptic curves. <p>-----</p> <p><i>The contribution of this Teaching Unit to the development and command of the skills and learning outcomes of the programme(s) can be accessed at the end of this sheet, in the section entitled "Programmes/courses offering this Teaching Unit".</i></p>
Evaluation methods	Assessment is based on an oral examination relating to theory and on the individual assignment carried out during the term, in equal parts. The examination tests knowledge and understanding of fundamental concepts and results, ability to solve problems and ability to draft the solutions with rigour and clarity.
Teaching methods	Learning activities consist of lectures which aim to introduce fundamental concepts, to explain them by showing examples and by determining their results, to show their reciprocal connections and their connections with other courses in the programme for the Bachelor in Mathematics. Students are assigned problems every two weeks, on which they will deliver a written report at the end of the semester.
Content	<p>In 2018-2019, we will study compact Riemann surfaces and their link with algebraic curves. Riemann was the first to understand that algebraic functions like "square root of z" are well defined and meromorphic on a branched covering of the complex plane with a point added at infinity. The concept was clarified only fifty years later by Hermann Weyl who introduced the notion of an abstract variety. We shall study the following topics:</p> <ol style="list-style-type: none"> 1. Abstract Riemann surfaces, construction of the Riemann sphere. 2. Construction of the Riemann surface of an algebraic function, determination of its genus. 3. Elliptic curves. 4. Applications to mathematical physics. <p>We will illustrate the theory with many examples taken in particular from the theory of elliptic curves, which are topologically tori with one hole (genus 1 compact Riemann surfaces).</p> <p>Today Riemann surfaces and algebraic curves play a fundamental role in the theory of integrable systems, in quantum field theory as well as in number theory. Some of these themes will be considered in the master class LMAT2260.</p>

Inline resources	The Moodle website provides a course outline, bibliographical references, as well as the problem sets to be done during the semester.
Bibliography	Roger Godement, Analyse mathématique III, Springer 2002, chapitre 10. Otto Forster, Lectures on Riemann Surfaces, Springer GTM 81, 1981, chapter 1.
Faculty or entity in charge	MATH

Programmes containing this learning unit (UE)				
Program title	Acronym	Credits	Prerequisite	Aims
Additionnal module in Mathematics	LMATH100P	5		