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JOINT MODELLING OF REPEATED MEASUREMENTS AND EVENT TIME: APPLICATION OF SURVIVAL AND PERFORMANCE TRAITS OF LAMBS BRED IN SUB-HUMID TROPICS

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Joint Modelling of repeated measurements and event time: Application to survival and performance traits of lambs bred in sub-humid tropics

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Abstract

We consider the analysis of a study for Dorper, Red Maasai and crossbred lambs born over a period of 6 years at Diani Estate, Kenya. The study was designed to compare survival and performance traits of genotypes with differing susceptability to helminthiasis. The available data include information on time to death and repeated measurements of body weight, packed cell volume (PCV) and faecal egg count (FEC) for the animals. In the paper we consider joint modelling of the survival time and the repeated measurements. Such an approach allows to account in the analysis the possible asociation between the survival and repeated measurement processes, what offers several advantages. In the paper, the advantages and limitations of the joint modelling are dicussed and illustrated using the Diani Estate study data.

Key Words: repeated measurements, time-to-event, joint modelling, sheep, helminthiasis.

1 Introduction

The data used in this study come from an animal breeding experiment carried out by the International Livestock Research Institute (ILRI) from 1991 to 1996 [1] at Diani Estate, Kenya Coast. The objective of the experiment was to study genetic resistance to naturally acquired gastro-intestinal nematodes in different breeds of sheep, namely the Red Maasai (found in East Africa and perceived to be resistant to helminthisis), Dorper (originating from South Africa and presumed to be susceptible) and their cross breeds. Three ewe genotypes (Dorper, Red Maasai, and Red Maasai \times Dorper) were mated to Dorper and Red Maasai rams in single-sire mating groups in a diallel design to generate two pure-bred and four cross-bred genotypes. The data collected during the study consisted of repeated measurements of the traits: body weight (BWT), packed cell volume (PCV) and faecal egg count (FEC), which were measured periodically over a lamb's first one year of life. Overall, 1745 lambs were born alive during the six-year period of the study. The repeated measurements, however, were highly unbalanced as 655 (38%) of the lambs died and 92 (5%) were stolen before they reached one year of age.

Assessment of the level of genetic resistance has been carried out by Baker et al. [1, 2], by applying linear mixed models to individual measurements of the traits, that were recorded from birth to one year of age. In the analysis undertaken by these authors only the information on the animals that survived to each of the analysed time points was utilised. Nguti et al. [14] used these same traits in a frailty model for survival, where correlation was induced among the ages at time of death for lambs from the same sire. In that analysis, PCV and FEC were separately included in the model as time-varying covariates, with either a baseline or time-varying BWT. One handicap of this latter analysis was that the measured traits were only recorded at monthly time points, and were thus unknown at the time of death. To overcome this problem, the nearest preceding measured value of the trait was used to

impute for the value at the time of death, resulting in a piecewise constant process. In addition, the analysis did not correct for the possible measurement error in the measurements of BWT, PCV and FEC. Such error can result from both the analytical error and short-term, biological variability. Failure to account for the measurement error and for any missing timevarying covariate observations, has been shown to cause the estimated regression parameters in the Cox proportional hazard (PH) model to be biased towards the null [4, 16].

In the described study, as in many longitudinal studies where individuals are followed over time, the data can be grouped into three categories: (1) the elapsed time to an event such as death; (2) repeated measurements of time-varying variables (like PCV, FEC, BWT); (3) time-varying (e.g., rainfall) or constant baseline (e.g., sire, breed) covariates that may affect both the repeated measurement and the time-to-event processes. When modelling of the repeated measurements is of interest, one may focus, for instance, on how the measurements change with time, how the parameter estimates are influenced by drop-out of individuals during the course of the study, or on how the measurements may be affected by the additional covariates. Looking at things from a time-to-event process point of view, the interest may focus on, e.g., how the time to the event is affected by both the repeated measurement process and the additional covariates. A vast amount of literature exists on the methods suitable for either approach. To analyse event-time data parametric or non-parametric models can be used, but the Cox PH model is often the method of choice. Repeated measurements are commonly analysed using linear mixed effects models [11]. These models are attractive for several reasons, one of them being the ability to easily accommodate unbalanced designs, especially regarding the timing and frequency of observations. The models also allow for an explicit partitioning of variability and estimation of individual effects. In particular, at least two sources of variability are readily identified: between- and within-individual variation. The between-individual variability is often modelled by a vector of correlated, individual random effects.

In the last ten years many methods, which simultaneously use the information available in both the time-to-event and the repeated measurement processes, have been proposed in medical research. In particular, several models have been developed in the area of acquired immunodeficiency syndrome (AIDS) research [5, 7, 17, 19, 21] and in schizophrenia studies [9, 22]. A detailed review of research work in joint modelling of times to an event and repeated measurements is given in reference [20]. Several advantages of joint modelling of the repeated measurement and the time-to-event processes have been highlighted in the literature: (1) the repeated measurements can be extrapolated from the observed measurement times to the specific event time in a way that utilises the entire measurement history; (2) the time-to-event is allowed to depend on the 'true' but unknown value of the repeated measurement, thus making an adjustment for the measurement error, which in turn leads to reduced bias of the parameter estimates of the Cox model; and (3) the repeated measurement process is adjusted for any loss of information arising from death or loss of individuals.

The objective of the current paper is to use the joint modelling approach to model the time to death and the repeated measurements of PCV, BWT and FEC. To this aim, the methodology proposed by Henderson et al. [9] is used. The need for joint models to model survival and performance traits in animals studies is discussed in [6]. The paper is organised as follows. In Section 2 more details on the motivating dataset are given. Section 3 provides a brief background on the linear mixed effects and the Cox PH models, as well as the joint model of Henderson et al. [9]. In Section 4 we adopt the joint model to the analysis of the motivating dataset. Results are presented in Section 5 and discussed in Section 6.

2 Motivating data

Measurements of PCV, FEC and BWT were taken from lambs from birth to one year of age in batches of lambs born in each of the years 1991 to 1996. Packed cell volume and FEC were measured according to methods reported by Baker et al. [1]. All lambs were weighed at birth and their BWT, PCV and FEC subsequently recorded at one and two months of age. On either of these latter occasions, when individual lambs had a FEC greater than or equal to 2,000 eggs per gram (epg) and/or a PCV less than or equal to 20%, they were treated (drenched) with an anthelmintic drug. Lambs with low PCV were also checked for trypanosome infections. At about three months of age, when weaned, the lambs were again weighed, and blood and faecal samples collected for PCV and FEC, respectively. All lambs were then drenched. The lambs were then left to graze on pasture, separately from the ewes and rams. Every week a monitor group of about 50 lambs, made up of approximately equal numbers of lambs of each genotype and sex, was sampled and their mean FEC recorded. If the mean FEC was over 2,000 epg then, during two consecutive days, all lambs were weighed, faeces and blood samples taken and the lambs drenched. This procedure was followed until the lambs reached on average one year of age. This procedure resulted in five drenchings in each year except 1994 and 1996. In 1994, the year with the highest rainfall, the lambs were drenched eight times post-weaning, while in 1996 six drenchings occurred.

3 Methodology

In this section we first briefly discuss the methods used in (separate) modelling of repeated measurements and time-to-event data. Then we shortly review joint modelling.

3.1 Linear mixed effects models for repeated measures

Data sets resulting from follow-up studies are often highly unbalanced, with subjects having unequal number of measurements. Moreover, the data have complex correlation structure

due to repeated measurements for each individual. As a result such data are not ideally suited to analysis by classical least squares techniques and linear mixed effects models [11] are now standard tools for analysing such complex hierarchical data.

Let Y_{ij} denote the observed jth measurement for the *i*th individual recorded at time t_{ij} $(i = 1, \ldots, N; j = 1, \ldots, n_i)$ and let $\boldsymbol{Y}_i^T = (Y_{i1}, Y_{i2}, \ldots, Y_{in_i})$. Then a linear mixed effects model is written as

$$
\boldsymbol{Y}_i = \boldsymbol{X}_{1i}\boldsymbol{\beta}_1 + \boldsymbol{Z}_i\boldsymbol{b}_i + \boldsymbol{\varepsilon}_i,\tag{1}
$$

where X_{1i} and Z_i are $n_i \times p$ and $n_i \times q$ design matrices, respecitvely, β_1 is a $p \times 1$ vector containing the fixed effects, and b_i is a $q \times 1$ vector of the random effects. It is assumed that \mathbf{b}_i is $N(\mathbf{0}, \mathbf{D})$, i.e., it is normally distributed with mean zero and variance-covariance matrix $\mathbf{D} = [d_{kl}]$, where $d_{kl} = \text{Cov}(b_{ik}, b_{il})$. Furthermore, it is assumed that b_i is independent from the vector of residual random errors ε_i . The residual errors are assumed to be $N(0, \Sigma_i)$, with variance-covariance matrix Σ_i depending on i only via its size $(n_i \times n_i)$. It then follows that, marginally, Y_i is normally distributed with mean $X_{1i}\beta_1$ and variance-covariance matrix $V_i = Z_i \mathbf{D} Z_i^T + \Sigma_i$. In model (1) Σ_i captures the within-individual variability while the between-individual variability is modelled through the random effects b_i . In particular if

$$
\pmb{Z}_i^T = \left(\begin{array}{cccc} 1 & 1 & \ldots & 1 \\ t_{i1} & t_{i2} & \ldots & t_{in_i} \end{array} \right)
$$

then model (1) is known as a random intercepts and slopes model (see reference [18], p. 25). The underlying assumption of this model is that the measurements increase linearly in time, but for each individual the linear trend has its own intercept and slope. Further, we have, if $Var(\epsilon_{ij}) = \sigma^2$, the result that the assumed covariance function of the response for this model is

$$
Cov(Y_{ik}, Y_{il}) = d_{11} + d_{22}t_{ik}t_{il} + d_{12}(t_{ik} + t_{il}) + \mathbf{1}(k = l)\sigma^2,
$$
\n(2)

where $\mathbf{1}(A)$ is the indicator function of event A. Note that function (2) is quadratic over time.

Model (1) has been used extensively to analyse repeated measurements arising from animal breeding programs [8, 10, 12, 13]. In these applications more emphasis has been placed on the covariance structure of the random effects (b_i, ε_i) in order to capture different sources of variability, such as those due to maternal, paternal and environmental effects.

To estimate the parameters of model (1), various approaches can be applied. The most commonly used is the classical method of maximum likelihood (ML), which results in generalised least square (GLS) estimates for β . This method of estimation however leads to underestimation of the variance parameters involved in \bm{D} and $\bm{\Sigma}_i$. As an alternative, the restricted maximum likelihood estimation (REML) can be used, which remedies this problem [18].

3.2 The Cox proportional hazard model

Let the *i*th individual $(i = 1, ..., N)$ be observed from a time zero to a failure time T_i or to a potential right censoring time C_i . Let $T_i^o = \min(T_i, C_i)$, be the observed time and δ_i be the censoring indicator which is equal to 1 if $T_i^o = T_i$ and 0 otherwise. Hence the observed data for the *i*th subject are (T_i^o, δ_i) . The basic analytical quantities for time-to-event data are the survivor function

$$
S(t) = Pr(T \ge t),
$$

which is the probability of surviving beyond time t , and the hazard function

$$
\lambda(t) = \lim_{\Delta t \to 0^+} \frac{Pr(t \le T < t + \Delta t | T \ge t)}{\Delta t},
$$

which is the instantaneous failure rate after surviving up to time t . In most time-to-event studies interest focuses on how the hazard function is affected by independent covariates. To assess this effect, Cox [3] has proposed the following model:

$$
\lambda_i(t) = \lambda_0(t) \exp(\boldsymbol{x}_{2i}^T \boldsymbol{\beta}_2),\tag{3}
$$

where $\lambda_0(t)$ is the baseline hazard function common to all individuals, x_{2i} is a $p \times 1$ vector of the observed covariates for the *i*th individual, and β_2 is the corresponding vector of regression

parameters to be estimated. Model (3) is known as the Cox proportional hazard model and has been used extensively in the last three decades in the analysis of failure-time data.

3.3 A joint model for repeated measurements and time-to-event

Let $\boldsymbol{Y}_i^T = (Y_{i1}, Y_{i2}, ..., Y_{in_i})$ be the vector of the repeated measurements for the *i*th individual measured at times $t_i^T = (t_{i1}, \ldots, t_{in_i})$. Let $T_i^o = \min(T_i, C_i)$ and δ_i denote, respectively, the time-to-event and the censoring indicator for the ith individual. The observed data available for the *i*th individual are thus $(T_i^o, \delta_i, Y_i, t_i, X_{1i}, x_{2i})$, where X_{1i} denotes the matrix of the observed values of covariates believed to influence the repeated measurements \boldsymbol{Y}_i , while x_{2i} is a vector of the observed values of covariates believed to affect the time-to-event process.

Henderson et al. [9] have proposed a model for the joint analysis of both the time-to-event and repeated measurements. They postulate a latent (unobserved) bivariate Gaussian process $W_i(t) = \{W_{1i}(t), W_{2i}(t)\}\$ such that the repeated measurements process depends on $W_{1i}(t)$ and the event time process on $W_{2i}(t)$. In particular, for the repeated measurements process, consider a model of the general form

$$
\boldsymbol{Y}_i = \boldsymbol{\mu}_i(t_i) + \boldsymbol{W}_{1i}(t_i) + \boldsymbol{\epsilon}_i, \tag{4}
$$

where ϵ_i is an $N(0, \Sigma_i)$ error vector such that Σ_i is a diagonal matrix and $Var(\epsilon_{ij}) = \sigma_e^2$. Note that in (4), we use $\mu_i(t_i)=(\mu_i(t_{i1}),\ldots,\mu_i(t_{in_i}))^T$ and $\bm{W}_{1i}(t_i)=(W_{1i}(t_{i1}),\ldots,W_{1i}(t_{in_i}))^T$ as shorthand notation. Further, $\mu_i(t_i)$ is the systematic component, which can be described by a linear model, e.g., $\mu_i(t_i) = X_{1i}\beta_1$. As a basic example for the latent process $W_{1i}(t)$, Henderson et al. [9] consider

$$
W_{1i}(t) = U_{1i} + U_{2i}t,\t\t(5)
$$

where (U_{1i}, U_{2i}) is a bivariate normal random vector with zero mean and variance-covariance

$$
\boldsymbol{D}_1 = \begin{pmatrix} \sigma_1^2 & \sigma_{12} \\ \sigma_{12} & \sigma_2^2 \end{pmatrix}.
$$

One can observe that $\mu_i(t)$ in model (4) corresponds to $X_{1i}\beta$ in model (1), while $W_{1i}(t)$ corresponds to $\mathbf{Z}_i \mathbf{b}_i$, with $\mathbf{b}_i \equiv (U_{1i}, U_{2i})^T$.

On the other hand, the time-to-event is modelled through a Cox proportional hazard model

$$
\lambda_i(t) = \lambda_0(t) \exp \left\{ \boldsymbol{x}_{2i}^T \beta_2 + W_{2i}(t) \right\}.
$$
\n
$$
(6)
$$

It is assumed that the repeated measurement and time-to-event processes are conditionally independent given $W_i(t)$. However, in order to induce association between the two processes, $W_{2i}(t)$ is taken to be related to particular components of $W_{1i}(t)$. This is achieved via the general equation

$$
W_{2i}(t) = \gamma_1 U_{1i} + \gamma_2 U_{2i} + \gamma_3 W_{1i}(t). \tag{7}
$$

For example, a joint model with $W_{2i}(t) = \gamma_1 U_{1i} + \gamma_2 U_{2i}$, would allow both the random intercept U_{1i} and slope U_{2i} , involved in (5), to affect the risk of the event.

The parameters of the models for the repeated measurement process and the time-to-event process are estimated jointly by maximising the observed joint likelihood of the data, as described in references [20, 21].

4 Application

We now describe the application of the joint model described in the previous section to the data introduced in section 2. Separate analyses of the repeated measurements of PCV, FEC and BWT were performed. Survival times of lambs that survived beyond one year, or those of lambs that were stolen, were censored at one year and at the last recorded observation, respectively.

Nguti et al. [14] reported an average lamb mortality of 19% in the pre-weaning period and 31% in the post-weaning period. The age at death during the post-weaning period ranged from 3 to 12 months (median 6.4 months). The number of repeated measurements recorded from weaning ranged from 1 to 8 (median 6) per lamb with 1994 having the most postweaning measurements. Figures 1 to 3 show scatter plots of the measurements recorded from one to 12 months for PCV and FEC and those from birth to 12 months for BWT across the six years. In each plot individual profiles for a randomly selected sample of 15 lambs are highlighted. Although all animals were weighed and sampled on the same day, ages varied as a result of lambs being born within a period of about 20-40 days.

FIGURE 1 and 2 ABOUT HERE

In the joint models with either PCV, BWT or FEC as repeated measurements, fixed effects of genotype (6 levels), year of birth (6 levels) and sex (2 levels) were included in the repeated measurements component of the joint model. As suggested by Figures 1—3, each of the traits was assumed to be curvilinear over time. Age of dam (5 levels) was considered as a baseline covariate for the time-to-event component only, but not for the repeated measurements, where it was found not to be significant.

Consequently, we can define $\boldsymbol{\beta}_1^T = [\mu, \boldsymbol{\beta}_0^T]$, where $\boldsymbol{\beta}_0^T = [\alpha_1, \alpha_2, \alpha_3, \alpha_4, \alpha_5, \varsigma_1, \varsigma_2, \varsigma_3, \varsigma_4, \varsigma_5, \varpi_1]$, α_m $(m = 1, \ldots, 5)$ are the binary indicators capturing the breed effects, ς_k $(k = 1, \ldots, 5)$ are the indicators for year of birth effects and ϖ_l is the binary indicator for males. As a result, the repeated measurements model can be written as

$$
\boldsymbol{Y}_i = \boldsymbol{X}_{1i}\boldsymbol{\beta}_1 + \eta_1\boldsymbol{t}_i + \eta_2\boldsymbol{t}_i^* + \boldsymbol{W}_{1i}(\boldsymbol{t}_i) + \boldsymbol{\epsilon}_i,\tag{8}
$$

where X_{1i} is the $n_i \times 12$ design matrix corresponding to β_1 , (η_1, η_2) are the parameters associated with the time trend, $t_i^{*T} = (t_{i1}^2, \ldots, t_{in_i}^2)$ is the vector of the quadratic times, and $\boldsymbol{W}_{1i}(\boldsymbol{t}_i)^T = \{W_{i1}(t_{i1}), \ldots, W_{in_i}(t_{in_i})\}$. Let $\boldsymbol{\beta}^T = (\boldsymbol{\beta}_1^T, \eta_1, \eta_2)$, and $\boldsymbol{X}_1(\boldsymbol{t}_i) = (\boldsymbol{X}_{1i} | \boldsymbol{t}_i | \boldsymbol{t}_i)$ be the $n_i \times 14$ design matrix corresponding to β . Model (8) can then be re-written as

$$
\boldsymbol{Y}_i = \boldsymbol{X}_1(t_i)\boldsymbol{\beta} + \boldsymbol{W}_{1i}(t_i) + \boldsymbol{\epsilon}_i. \tag{9}
$$

FIGURE 3 ABOUT HERE

To specify the survival component of the joint model, let $\beta_2^T = [\beta_0^T, a_1, a_2, a_3, a_4]$, where a_r ($r = 1, \ldots, 4$) are the binary indicators coding the dam age groups (with levels: ≤ 2 years, 3, 4, 5 and \geq 6 years). The model for survival time is then given by

$$
\lambda_i(t) = \lambda_0(t) \exp\left\{ \boldsymbol{x}_{2i}^T \boldsymbol{\beta}_2 + W_{2i}(t) \right\},\tag{10}
$$

where X_{2i} is the $n_i \times 15$ design matrix associated with β_2 .

For all the three traits the following settings for W_{1i} and W_{2i} were considered:

- (S1) $W_{1i}(t) = U_{1i}$, $W_{2i} = 0$;
- (S2) $W_{1i}(t) = U_{1i} + U_{2i}t$, $W_{2i} = 0$;
- (S3) $W_{1i}(t) = U_{1i}$, $W_{2i} = \gamma W_{1i}$;
- (S4) $W_{1i}(t) = U_{1i} + U_{2i}t$, $W_{2i} = \gamma_1 U_{1i} + \gamma_2 U_{2i} + \gamma_3 W_{1i}(t)$.

Settings (S1) and (S2) assume independence between the repeated measurement and survival processes. Settings (S3) and (S4) correspond to (S1) and (S2), respectively, with respect to the structure of $W_{1i}(t)$, but allow for dependence between the processes (joint models). To obtain parameter estimates for the fixed effects, variance components and the association parameters of the joint models (S3) and (S4) specified above, a program in SAS was written. Estimates from either setting (S1) and (S2) were computed using PROC MIXED (for repeated measurements) and PROC PHREG (for survival time) in SAS.

Estimates of the standard errors for all parameter estimates in the joint models were obtained by using the jackknife method. This was achieved by leaving out the observations for lambs from the same sire and then re-fitting the model to the remaining observations. Classically, jackknife provides reliable estimates of the standard errors if the observations omitted are independent from those that are left in. When observations for lambs from the same sire are left out, so is the genetic component of these lambs. This genetic component is assumed here to provide more individual contribution to the lamb characteristics (e.g. survival, BWT) than the common enviromental components, which are shared by lambs born in the same year. This is supported by the findings in reference [2]. These authors show that for the analysed data set, the differences observed in heritability estimates of PCV and FEC for Dorper- compared with Red Masaai-sired lambs were more likely due to the differences in genetic variance rather than in environmental variability.

5 Results

Below the results of the fitted models for PCV, BWT and FEC for the above settings are reported. For each trait the results of the joint model are compared with those of the corresponding independence model for both the repeated measurements and survival estimates.

5.1 Packed cell volume from one month

Initally, the analysis of the repeated measurements for PCV from one month until one year of age was considered. When fitting the model corresponding to setting (S2), a non-positive definite estimate of the variance-covariance matrix D_1 (see Section 3.3) was obtained. On further investigation, it was discovered that the PCV repeated measurements were negatively correlated, with the correlation increasing in the absolute value over time. This negative serial correlation cannot be captured by a model with a random intercept and random slope, as specified under setting (S2). In particular, taking into account the magnitude of the correlation and low variability of the slopes of individual profiles, the variance of the random slope is estimated to be less than or equal to 0, which is obviously an inadmissible value. Therefore, for the PCV measurements collected from one month to one year of age, the models for settings (S2) and (S4) could not be fitted. On the other hand, the models for settings (S1) and (S3), which do not account for the negative correlation, could be used. The results for these models are given in Table 1. Strictly speaking, one should treat the results with caution since they are based on models with a possibly misspecified variance-covariance structure.

TABLE 1 ABOUT HERE

Setting (S1): Under this setting, which assumes independence between PCV measurements and survival time, the Dorper (DxD) breed had the lowest mean PCV from one month to one year of age, which was between 0.1 to 1.9% units lower than for other genotypes (see the 'Repeated measurements model - S1' column in Table 1). This difference increased as the Red Maasai genotype in the lambs increased, with the Red Maasai having the highest mean PCV. The linear and quadratic time effects were both significant $(P<0.001)$ implying an average non-linear trend in PCV. The trend is as indicated in Figure 1, which shows a general sharp decline in PCV after one month in all years except 1996 followed by a slight rise. The lambs born in 1992-1995 had on average a lower PCV (0.3 to 3.2%) units than those born in 1991. The mean PCV was the highest in 1996. On average, male lambs had lower PCV than female lambs.

By exponentiating the estimates given in the 'Survival model - S1' column in Table 1, one can see that, as compared to the Dorper, the relative mortality hazard of the other genotypes ranged from $\exp(-0.476) = 0.62$ to $\exp(-1.34) = 0.26$. The Rx(RxD) and RxR breeds had the lowest, and similar, mortality. The hazard of the lambs born in the years 1993—1996 was statistically significantly higher than that of the lambs born in 1991 and ranged from 2.2 to 4.0. Male lambs had a higher mortality hazard than females while the hazard ratio decreased with increasing age of dam.

Setting $(S3)$: This setting corresponds to $(S1)$, but assumes dependence between PCV measurements and survival time. As compared with (S1) the differences in the mean PCV, relative to the Dorper breed, increased slightly for all other genotypes. For instance, the estimated mean PCV for the non-Dorper genotypes was 0.2-2.2% units higher than for the Dorper breed (see the 'Repeated measurements model - S3' column in Table 1). This increase might be the result of the adjustment of the analysis of the repeated measurements for the variation in death rates. The estimated time trend parameters for the repeated measurements model for (S1) setting were similar to those obtained for (S3).

Relative to the mortality hazard for the Dorper breed, the hazard ratio for the non-Dorper genotypes now ranged between 0.60 to 0.24, as compared to (S1) setting (see the 'Survival model - S3' column in Table 1). Significant negative estimates (P<0.001) were obtained for the association parameters (γ in Table 1) for the survival model under (S3). This indicates that the mortality hazard decreased with increasing PCV.

5.2 Packed cell volume from weaning

As the critical period for assessing genetic resistance to endoparasites in lambs is between weaning and 12 months of age [1], the analysis of the PCV repeated measurements for the period from weaning onwards was also considered. In this analysis, the survival time was re-defined by using weaning as the time of origin. Consequently, in this analysis only the animals alive at the time of weaning were considered. The results for settings (S1)—(S3) and (S2)—(S4) are given in Tables 2 and 3, respectively.

Settings (S1) and (S2): For $(S1)$, similar trends in the repeated measurement model, as those reported for the analysis of data from one month of age (see Table 1), were observed when PCV measurements were considered from weaning (see Table 2). However, unlike for the period from one month of age, the time trend had a more moderate negative slope estimate. This corresponds to Figure 1, which shows a more gradual decline in PCV after weaning than before.

TABLE 2 ABOUT HERE

The relative mortality hazard in the post-weaning period exhibited similar pattern as in the analysis of data from one month of age, but now the Rx(RxD) had the lowest mortality $(exp(-1.641) = 0.19)$ when compared to the Dorper breed. The hazard of the lambs born in the years 1993—1995 was now five times higher while it was 70% higher for lambs born in 1996 when compared to lambs born in 1991.

In the repeated measurements model with both random intercepts and slopes, i.e. under (S2) setting (see the 'Repeated measurements model - S2' column in Table 3), similar trends for the fixed effects parameter estimates were observed as in the simpler, random-intercept-only model (see the 'Repeated measurements model - S1' column in Table 2). However, in the former, the ranges of the estimates were reduced. In the model under (S2) setting the random intercept and slope were negatively correlated ($\sigma_{12} = -1.82$). This implies that lambs with a high PCV at weaning had a more rapid decline in PCV than those with a low PCV. The estimated variance component for the random intercept (σ_1^2) was more than 2 times larger in $(S2)$ than in the simpler model $(S1)$. Note, however, that, according to equation (2) , the negative correlation between random intercept and slope will reduce the total variability under (S2) setting, making it similar to the sum of σ_1^2 and σ_e^2 in the simpler (S1) model. It is also worth noting that, according to equation (2), under (S2) covariance between two PCV measurements depends on time, and can be negative if the correlation between random intercept and slope is negative. Since it is possible that the correlation between PCV measurements may change in time and may be negative (see remarks in Section 5.1), this gives more credibility to the results obtained for (S2) and (S4) settings, because the models used in (S1) and (S3) impose a constant positive correlation between PCV measurements.

TABLE 3 ABOUT HERE

Settings (S3) and (S4): As compared with (S1) and (S2) settings, the differences in the mean PCV for all other genotypes , as compared with the Dorper breed, increased slightly in the joint models constructed under both (S3) (see the 'Repeated measurements model - S3' column in Table 2) and (S4) (see the 'Repeated measurements model - S4' column in Table 3) settings. For instance, for (S3) setting (Table 2), the estimated mean PCV from weaning for the non-Dorper genotypes was 0.6-3.4% units higher than for the Dorper breed. For (S4) setting (Table 3), the difference was between 0.3% and 3.0%. An increase that might be attributed to the adjustment of the analysis of the repeated measurements for the variation in death rates.

Relative to the mortality hazard for the Dorper breed, the hazard ratio for the non-Dorper genotypes now ranged from 0.55 to 0.16 for both (S3) and (S4) settings (see the 'Survival model - S3' column in Table 2 and the 'Survival model - S4' column in Table 3). These estimates are lower than the estimates obtained for the corresponding (S1) and (S2) survival models. For (S3) setting the mortality hazard for lambs born in 1993—1995 was about five times higher than in 1991 (Table 2). For (S4) the ratio was about five for 1993, while for 1994 and 1995 it was about four times, a lower ratio than for (S3). This would appear to be supported by Figure 1. The lambs born in 1994 and 1995 had much lower PCV measurements at weaning than those born in 1991, and PCV has been shown to correlate with pure survival. However, the former, PCVs increased over time while those for the latter decreased. Thus, adjusting for the PCV evolution over time results in a slight decrease in the mortality hazard for 1994—1995. On the other hand, the lambs born in 1993 and 1991 had almost similar PCV measurements at weaning. The decrease in 1993 over time was, however, much sharper (larger negative slope) than in 1991. Adjusting for this decrease translates into a higher mortality hazard for 1993. Finally, higher hazard ratios are observed for 1994 and 1995 in (S3) than (S4), since the latter model adjusts the risk only for the overall level of PCV over time (without adjusting for the rate of change).

Significant negative estimates (P<0.001) were obtained for all the association parameters (γ in Table 2, and $\gamma_1-\gamma_3$ in Table 3) for the survival model under both (S3) and (S4) settings. This indicates that the mortality hazard decreased with increasing PCV. Thus, after weaning in (S3) setting, lambs with PCV measurements higher than the average had a lower mortality hazard than those with lower PCV measurements. The standard deviation of the distribution of the random intercepts in the repeated measurements part of the joint model for (S3) setting was estimated to equal $2.51(=\sqrt{6.318}$ - see Table 2). Thus, the model predicts that for a (random) increase of PCV due to an increase of the random intercept $W_{1i} = U_{1i}$ by one standard deviation, the risk of death decreases by $\exp(-\gamma * W_{1i}) = \exp(-0.303 * 2.51) = 0.47$ (see Table 2). For the (S4) model a large negative estimate was obtained for γ_2 , which corresponds to the random individual slope. Thus, the model indicates that at any time, lambs that had large decrease in PCV had increased risk of death.

5.3 Body Weight

Measurements of body weight from birth to one year of age were used in this analysis. Models were fitted using all four settings. The parameter estimates of the fixed effects were similar for $(S1)$ – $(S3)$ and $(S2)$ – $(S4)$ settings. We thus report only the estimates of the models constructed under (S2) and (S4) setting, which are shown in Table 4.

Setting (S2): The Dorper (DxD) breed had the highest mean BWT, which was between 0.04 to 0.72 kg higher than for other genotypes (see the 'Repeated measurements model - S2' column in Table 4). There was a non-linear trend in change of the body weight over time. On average, the lambs born in 1994—1996 were lighter than those born in 1991. Male lambs were on average 0.11 kg heavier than the females.

Compared with the Dorper the relative mortality hazard of the other genotypes ranged from 0.61 to 0.27, with the Red Maasai (RxR) and $Rx(RxD)$ having the lowest hazard. As for the previous PCV analyses, an increased mortality hazard was noted for the years 1993—1996. Lambs born to ewes $>$ 3 years of age had lower hazard than those born to younger ewes.

TABLE 4 ABOUT HERE

Setting $(S4)$ *:* Adjusting the repeated measurement process for the variation in death rates had a only slight effect on the parameter estimates of the (S4) models when compared to (S2) setting.

The relative mortality of the genotypes now ranged from 0.61 to 0.24 with the RxR genotype having the lowest hazard mortality. This result indicates that despite being lighter in body weight when compared to the other genotypes the Red Maasai demonstrates better performance in terms survival. The age of dam effect was non-significant. This could be due to the fact that in this analysis, we account for the low body weight of lambs born to young dams, which biologically is due to low milk production of the dam in her first parity.

Negative estimates of the parameters relating the random components of the repeated measurements model to the survival model were observed (see the estimates for $\gamma_1-\gamma_3$ in Table 4). In particular, there was a significant negative association only between random growth rate $(\gamma_2, P<0.001)$ and risk of death. This shows that animals who had weight profiles with increasing slope had reduced risk of death. In a reduced model with γ_1 and γ_3 constrained to zero (results not shown), the estimates obtained for the association parameter γ_2 was $\hat{\gamma}_2 = -3.262$ (s.e.=0.389). The standard deviation of the random slope in this reduced model was equal to 0.22. Thus for every increase by one standard deviation, the mortality hazard associated to the rate of change in BWT was reduced by 0.49 (= exp(-3.262×0.22)).

5.4 Faecal Egg Count

The repeated measurements for FEC were log-transformed into $\text{LFEC} = ln(FEC + 25)$ as the data were highly skewed. Initially, an analysis of the repeated measurements from one month to one year of age was considered. As in the case with PCV, a negative correlation between repeated measurements, that increased over time, was observed. This problem precluded the estimation of any of settings $(S1)$ – $(S4)$. Considering only LFEC measurements from weaning onwards did not resolve the problem, as the negative correlation continued to persist among measurements collected towards the end of the one year period. The problem may be due to strong oscillations of the individual patterns that can be observed in the LFEC measurements in Figure 2 from one month onward, as well as from the time of weaning, that could be linked with the treatment protocol instigated in the study. A possible solution might be to extend the random structure (W_{1i}) of the repeated measurements model by including a serial correlation component in the model for repeated measurements process. Owing to the limitation in software availability, this modelling option was not attempted.

6 Discussion

The data discussed in this paper were previously analysed by Baker et al. [2] and Nguti et al. [14]. Baker et al. [2] analysed the repeated measurements of BWT, PCV and FEC without taking into account the survival pattern of the animals, and chose to analyse the data for each time point separately. They confirmed the higher resistance (lower FEC) and higher resilience (higher PCV) of Red Maasai than Dorpers. Nguti et al. [14], on the other hand, studied the survival of each genotype and introduced the effects of BWT, PCV and FEC as time-varying covariates in a shared frailty model, with the frailty defined as a random effect of sire. Introduction of PCV and FEC as time-varying covariates in that analysis in models with BWT (time-invariant or time-varying) reduced the magnitude of the sire variance, confirming the moderate levels of heritability reported by Baker et al. [2].

In the analysis presented in the current paper, individual repeated measurements were analysed jointly with the survival process. By doing so, parameter estimates in both components of the joint model in general increased in absolute order of magnitude, as compared with the models assuming independence beteen the two processes. For instance, in the joint model with PCV as the repeated measurement, the range of the mortality hazard ratios for different genotypes relative to the Dorper changed from 0.61—0.19 for (S1) and (S2) models to 0.55—0.16 for (S3) and (S4) models. Thus, adjustment for the evolution of PCV resulted in a clearer separation between the Dorpers and the Red Maasai. On the other hand, adjustment for the death rates widened the ranges of the parameters reflecting the differences among the various genotypes in PCV measurements. As shown by Baker et al. [2] the PCV values among the genotypes were similar at the first sampling at one month, prior to any significant of disease. The subsequent reductions in PCV were inversely correlated with levels of FEC, suggesting that the differences in overall mean PCV values among the genotype were more likely the result of the different levels of resistance between the Dorpers and the Red Maasai, rather than any genetic differences between breeds in their normal PCV values.

In general, repeated measurements such as PCV, BWT or FEC, are only recorded at specific time points. When such variables are used in a proportional hazards model as time-varying covariates, the standard method is to impute the missing observations by using the last observed value. This results in a piece-wise constant profile. This approach has been shown to lead to biased model parameters [16], with the presence of measurement error in the covariate attenuating the estimates towards zero. On the other hand, in the joint analysis, the repeated measurements are imputed by the 'true' values predicted under the model for the repeated measurement process. This reduces the attenuation and can explain the increase in the magnitude of parameter estimates observed for the joint models. In addition, the joint modelling allows other characteristics of the repeated measurements pattern, such as the rate of change (slope), to influence the risk of death. The effects of these characteristics is well demonstrated in this study when repeated measurements of PCV recorded from weaning were considered. Including a random slope had a major effect on the post-weaning risks of death for the years 1993 to 1995 when compared with 1991.

Nguti [15] compares the results from the survival component of the joint model under setting (S4) for the repeated measurements of PCV (from weaning) and BWT (from birth) together with those for a Cox PH model with a time-varying covariate for these measurements. Differences in hazard estimates are obtained by the two approaches. However, it would be erroneous to make direct comparisons of the two sets of results as the methodological aspects of the two models are different. The survival component of the joint model can be viewed as a conditional model (conditioned on the random effects which may be partially confounded with genotype), while a Cox PH model with a time-dependent covariate can be viewed as a population average model.

The aforementioned potential of the joint models for a more accurate analysis of the repeated measurements and survival processes is an attractive feature of the methodology. This potential, however, was reduced by the negative correlation limitations encountered in our data. These limitations need to be carefully reflected upon. For instance, it should be noted that the post-weaning measurements were obtained at the time lambs were diagnosed for treatment based on observations of the sentinel group of 50 lambs (see Section 2). Treatment will have resulted in decreases in FEC especially, and also increases in PCV. Thus data collected in between treatments, when measurements were more likely to have been within normal limits, were missing. These regular treatments are likely to have influenced the covariance structure resulting in the observed negative correlations. A similar problem occurred pre weaning when individual animals were treated on the basis of PCV and FEC. It should also be noted here that not all lambs that died did so due to helminthiasis. Although Nguti [14] found a survival rate differential between Dorper and Red Maasai regardless of whether deaths due to causes other than helminthiasis were omitted or not, the decreases in PCV and increases in FEC that are typical of the onset of helminthiasis may not have been reflected in deaths due to other causes. More frequent sampling and use of the data collected

mid-way between treatment interventions may have both understood better the patterns of changes in PCV and FEC in individual lambs and overcome the problem of negative correlation.

In the application of any statistical method one needs to be aware of the assumptions made. For example, in the joint models considered in this paper, the models used a bivariate Gaussian process to induce the association between the repeated measurements and the survival process. This, in turn, imposes a particular, hierarchical structure (e.g., random intercepts and slopes) of the model for the repeated measurements process. Such structure may not necessarily be adequate for a particular dataset. As already noted the models with random intercepts and random slopes were not able to capture the intrinsic patterns of FEC induced by the treatment interventions. On the other hand, they coped better with the BWT profiles from the time of birth. In general, random intercepts and slopes provide a representation of the dominant part of the evolution of the profiles, but do not capture a more subtle behaviour (e.g. short-term oscillations around an average pattern). Such a behaviour might be captured by using an autocorrelated stochastic processes. Henderson et al. [9] has proposed the use of a non-stationary Gaussian process in their approach. Unfortunately, due to the lack of appropriate software, this solution is not yet available in practice.

The joint models applied here did not allow for adjusting for correlations among survival times of lambs from the same sire. For this purpose, Nguti et al. [14] used frailty models with a random sire effect. In theory, the models formulated by Henderson et al. [9] allow for the inclusion of a frailty term in the time-to-event component of the joint model, but implementation needs to await development of appropriate software.

Conclusion

Classically, the effect of repeated measurements on the risk of death is assessed by treating the repeated measurement as a time-dependent covariate in a survival model. Estimates from

such an analysis have been shown to be biased towards zero, thus showing over-estimated hazard ratios. The bias can be removed by using joint models. This paper has illustrated the application of such models. Accounting for the survival (drop-out) mechanism has been observed to affect the parameter estimates related to the repeated measurements process.

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	Repeated measurements model				Survival model			
	S1		S ₃		S1		S ₃	
	est	s.e.	est	s.e.	est	s.e.	est	s.e.
Fixed effects								
Intercept	31.730	0.238	31.457	0.394				
time(months)	-2.856	0.052	-2.866	0.119				
time*time	0.217	0.005	0.217	0.011				
Genotype								
DxD	ref		ref		ref		ref	
Dx(DxR)	0.132	0.231	0.237	0.281	-0.476	0.121	-0.514	0.136
DxR	0.355	0.332	0.449	0.392	-0.569	0.172	-0.583	0.209
RxD	1.406	0.260	1.603	0.381	-0.872	0.169	-0.945	0.197
Rx(RxD)	1.668	0.224	1.935	0.313	-1.341	0.141	-1.390	0.184
RxR	1.937	0.279	2.230	0.356	-1.342	0.177	-1.407	0.226
Year of birth								
1991	ref		ref		ref		ref	
1992	-0.412	0.222	-0.373	0.303	-0.023	0.185	-0.048	0.209
1993	-0.340	0.219	-0.470	0.248	0.921	0.149	0.948	0.157
1994	-2.867	0.252	-3.098	0.270	1.358	0.167	1.361	0.185
1995	-3.178	0.251	-3.384	0.291	1.328	0.165	1.361	0.187
1996	1.097	0.257	1.008	0.306	0.724	0.197	0.769	0.248
Gender								
Females	ref		ref		ref		ref	
Males	-0.512	0.138	-0.558	0.156	0.220	0.088	0.232	0.115
Age of dam								
$\leq=2$ yrs				-	ref		ref	
$=3$ yrs		\overline{a}		$\bar{}$	-0.277	0.158	-0.271	0.160
$=4$ yrs		\overline{a}		$\bar{}$	-0.544	0.167	-0.505	0.181
$=5$ yrs		\overline{a}		$\overline{}$	-0.368	0.159	-0.278	0.182
$>= 6yrs$		\overline{a}		\overline{a}	-0.509	0.168	-0.461	0.150
Variances								
σ_e^2	25.817	0.398	25.905	$\,0.839\,$				
σ_1^2	3.037	0.283	2.804	0.327				
Association								
γ							-0.236	0.020

Table 1: Estimates from settings $S1$ and $S3$ for repeated measurements of $PCV(\%)$ from one month to 12 months and survival. and survival.

	Repeated measurements model			Survival model				
	S1		S ₃		S1		S ₃	
	est	s.e.	est	s.e.	est	s.e.	est	s.e.
Fixed effects								
Intercept	26.179	0.285	25.603	0.451		\overline{a}		
time (months)	-1.406	0.054	-1.419	0.084				
time*time	0.146	0.006	0.147	0.009				
Genotype								
DxD	ref		ref		ref		ref	
Dx(DxR)	0.361	0.287	0.563	0.399	-0.492	0.142	-0.584	0.190
DxR	0.978	0.412	1.140	0.580	-0.678	0.200	-0.707	0.293
RxD	1.756	0.318	2.206	0.465	-0.975	0.195	-1.169	0.242
R(RxD)	2.405	0.276	3.045	0.408	-1.641	0.176	-1.839	0.243
RxR	2.866	0.344	3.430	0.454	-1.332	0.201	-1.527	0.242
Year of birth								
1991	ref		ref		ref		ref	
1992	0.884	0.269	0.947	0.388	0.037	0.228	-0.077	0.278
1993	-1.160	0.263	-1.678	0.345	1.468	0.174	1.637	0.209
1994	-5.170	0.313	-5.678	0.466	1.570	0.203	1.640	0.252
1995	-5.666	0.310	-6.082	0.419	1.533	0.203	1.677	0.250
1996			1.901			0.268	0.458	0.276
Gender								
Females	ref		ref		ref		ref	
Males	-0.477	0.169	-0.616	0.212	0.300	0.104	0.342	0.150
		\overline{a}		$\overline{}$	ref	\overline{a}	ref	
		\overline{a}		$\overline{}$		0.177	-0.385	0.165
		\overline{a}		$\overline{}$				0.183
		\overline{a}		$\overline{}$				0.203
		\overline{a}		\overline{a}				0.209
								0.023
Age of dam \leq = 2yrs $=3$ yrs $=4$ yrs $=5$ yrs \geq 6yrs Variances σ_e^2 σ_1^2 Association γ	1.974 15.315 6.465	0.316 0.293 0.427	15.390 6.318	0.359 0.451 0.542	0.531 -0.377 -0.728 -0.549 -0.810	0.187 0.178 0.196	-0.669 -0.437 -0.698 -0.303	

Table 2: Estimates from settings S1 and S3 for repeated measurements of PCV (%) from weaning to 12 months and survival.

	Repeated measurements model			Survival model				
	S ₂		S4		S ₂		S ₄	
	est	s.e.	est	s.e.	est	s.e.	est	s.e.
Fixed effects								
Intercept	25.817	0.273	25.844	0.444		$\overline{}$		
time (months)	-1.465	0.052	-1.562	0.081		$\overline{}$		
time*time	0.160	0.006	0.164	0.009				
Genotype								
DxD	ref		ref		ref		ref	
Dx(DxR)	0.169	0.267	0.333	$\!0.354\!$	-0.492	0.142	-0.594	0.200
DxR	0.726	0.387	0.842	0.489	-0.678	0.200	-0.634	0.284
RxD	1.585	0.290	1.892	0.451	-0.975	0.195	-1.221	0.277
Rx(RxD)	2.070	0.254	2.521	0.404	-1.641	0.176	-1.843	0.257
RxR	2.586	0.319	2.991	0.440	-1.332	0.201	-1.569	0.304
Year of birth								
1991	ref		ref		ref		ref	
1992	1.460	0.237	1.392	0.404	0.037	0.228	-0.260	0.340
1993	-0.779	0.239	-1.208	0.358	1.468	0.174	1.678	0.282
1994	-3.685	0.286	-4.311	0.631	1.570	$\,0.203\,$	1.343	0.403
1995	-3.631	0.290	-4.285	0.661	1.533	$\,0.203\,$	1.396	0.471
1996	2.101	0.286	1.998	0.365	0.531	0.268	0.582	0.308
Gender								
Females	ref		ref	\overline{a}	ref		ref	
Males	-0.539	0.154	-0.597	0.188	0.300	0.104	0.357	0.170
Age of dam								
$\leq=2$ yrs		\overline{a}		$\qquad \qquad -$	ref	\sim	ref	
$=3$ yrs		$\overline{}$		\overline{a}	-0.377	0.177	-0.425	0.184
$=4$ yrs		\overline{a}		\overline{a}	-0.728	0.187	-0.685	0.205
$=5$ yrs		\overline{a}		\overline{a}	-0.549	0.178	-0.453	0.227
$>= 6yrs$		\overline{a}			-0.810	0.196	-0.676	0.213
Variances								
σ_e^2	12.901	0.272	12.641	0.401				
σ_1^2	15.894	0.990	15.380	1.517				
σ_{12}	-1.817	0.145	-1.590	0.236				
σ_2^2	0.276	0.024	0.261	0.028				
Association								
γ_1						$\overline{}$	-0.273	0.097
γ_2		\overline{a}				\overline{a}	-1.986	0.505
γ_3		\overline{a}					-0.251	0.087

Table 3: Estimates from settings S2 and S4 for repeated measurements of PCV(%) from weaning to 12 months and survival.

	repeated measurements model				Survival model			
	S ₂		S ₄		S ₂		S ₄	
	est	s.e.	est	s.e.	est	s.e.	est	s.e.
Fixed effects								
Intercept	4.662	0.103	4.665	0.146				
time (months)	2.330	0.016	2.229	0.045				
$time*time$	-0.101	0.001	-0.101	0.003		\overline{a}		
Gentotype								
DxD	ref	\overline{a}	ref		ref		ref	
Dx(DxR)	-0.036	0.103	-0.042	0.109	-0.494	0.108	-0.498	0.130
DxR	-0.405	0.150	-0.396	0.159	-0.630	0.157	-0.577	0.165
RxD	-0.058	0.117	-0.074	0.131	-0.809	0.149	-0.947	0.194
Rx(RxD)	-0.361	0.100	-0.391	0.125	-1.263	0.124	-1.221	0.160
RxR	-0.715	0.127	-0.727	0.142	-1.302	0.157	-1.404	0.203
Year of birth								
1991	ref	$\overline{}$	ref	\bar{a}	ref	$\overline{}$	ref	
1992	-0.621	0.102	-0.637	0.160	0.073	0.161	0.158	0.163
1993	0.504	0.100	0.647	0.138	0.763	0.136	0.017	0.219
1994	-1.852	0.120	-1.836	0.140	1.384	0.148	1.330	0.162
1995	-1.238	0.120	-1.167	0.145	1.246	0.149	0.968	0.188
1996	-2.033	0.118	-2.088	0.060	0.763	0.173	1.084	0.325
Gender								
Females	ref		ref		ref		ref	
Males	0.113	0.064	0.095	0.118	0.202	0.079	0.387	0.097
Age of dam								
$\leq=2$ yrs	ref	\overline{a}	ref	\overline{a}	ref		ref	
$=3$ yrs		\overline{a}	\overline{a}	$\bar{}$	-0.187	0.144	0.096	0.147
$=4$ yrs		\overline{a}	\overline{a}	$\frac{1}{2}$	-0.490	0.152	0.086	0.162
$=5$ yrs		\overline{a}		\overline{a}	-0.333	0.145	0.291	0.163
$>=$ 6yrs		\overline{a}		\overline{a}	-0.433	0.152	0.098	0.148
Variances								
	2.533	0.038	2.520	0.091		\overline{a}		
$\sigma_e^2 \over \sigma_1^2$	0.825	0.058	0.867	0.052		\overline{a}		
σ_{12}	0.179	0.013	0.221	0.017		\overline{a}		
σ_2^2	0.070	0.004	0.082	0.007		\overline{a}		
Association								
γ_1				\overline{a}	0.000	\overline{a}	-0.086	0.389
γ_2		\overline{a}		\overline{a}	0.000	\overline{a}	-3.285	1.609
γ_3		$\bar{}$		$\bar{}$	0.000	\overline{a}	0.006	0.079

Table 4: Estimates from settings $S2$ and $S4$ for repeated measurements of $BWT(kg)$ from birth and survival.

Figure 1: PCV measurements for the years 1991 to 1996. Bold vertical line indicates when the lambs were weaned.

Figure 2: Transformed log(FEC+25) measurements for the years 1991 to 1996. Bold vertical line indicates when the lambs were weaned.

Figure 3: Body weight measurements for the years 1991 to 1996. Bold vertical line indicates when the lambs were weaned.