



Signal Processing Seminars On the use of Gabor Filters in SOS Corrected Ultrasound Image Segmentation

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Small is big : Jeff Immelt is seen here unveiling the new Vscan technology (i.e portable Ultrasound) to the audience at Web 2.0 Summit in San Francisco (see http://www.gereports.com).

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A propagating wave partially reflects at the interface between tissues.

If these reflections are measured as a function of time, information is obtained on the position of the tissue

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The transmission mode converts an oscillating voltage into mechanical vibrations transmitted as pressure waves

Total pressure at position x is then given by $p_T(x,t) = p_0 + p(x,t)$ [Hill 04]

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Where $C \equiv \frac{1}{\sqrt{
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| Tissue type | Density (g/cm ²) | Speed of sound (m/s) |
|--------------------------------|------------------------------|----------------------|
| Connective | 1.120 | 1613 |
| Muscle | 1.050 | 1547 |
| Fat | 0.950 | 1478 |
| Adipose | 0.950 | 1450 |
| Blood | 1.060 | 1584 |
| Brain | 1.040 | 1560 |
| Breast | 1.020 | 1510 |
| Kidney | 1.050 | 1560 |
| Liver | 1.060 | 1595 |
| Muscle, cardiac | 1.060 | 1576 |
| Muscle, skeletal | 1.050 | 1580 |
| Skin | 1.090 | 1615 |
| Average soft tissue: Fatty | 0.985 | 1465 |
| Average soft tissue: Non-fatty | 1.055 | 1575 |
| Blood cells | 1.093 | 1627 |
| Blood plasma | 1.027 | 1543 |
| Spinal cord | 1.038 | 1542 |
| Spleen | 1.054 | 1567 |
| Testis | 1.044 | 1595 |
| Mean | 1.042 | 1557 |
| Standard deviation | 0.043 | 50 |

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Current Ultrasound devices assume that SOS is constant in all tissues (1540 m/s) [Fontanarosa 11]

In soft human tissues : $SOS = ((1.09) \cdot \rho + 0.419) \cdot 10^3 m/s \pm 3.5 m/s$

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Briefly, penetration depth in current devices is computed as $d = \frac{TOF}{2}S\tilde{O}S$ with $S\tilde{O}S = 1540 \text{ m/s}$ is the speed of sound (SOS)

Wherever actual penetration depth is given by $d_{corr} = \frac{1}{2} \sum_{j=1}^{n} SOS_{j}(TOF_{j} - TOF_{j-1})$

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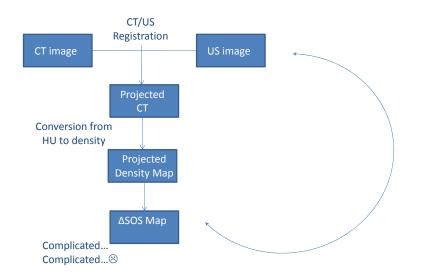
Wherever actual penetration depth is given by $d_{corr} = \frac{1}{2} \sum_{j=1}^{n} SOS_j (TOF_j - TOF_{j-1})$

And every voxel has to be resized in the axial direction from $d_i = \frac{1}{2}\tilde{SOS} \cdot (TOF_i - TOF_{i-1})$ to $d_{i,corr} = \frac{1}{2}SOS_i \cdot (TOF_i - TOF_{i-1})$

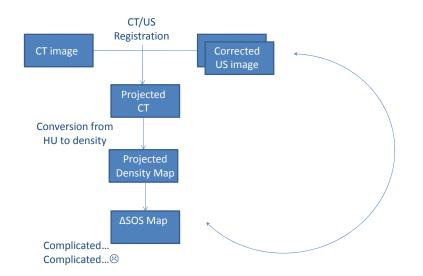
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The approach consists of 2 steps :

Training

Application

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During training, shape and tecture priors are extracted from training images

Then an anisotropic median filtering is applied to reduce the speckle noise from the test images

■ Finally Support vector machines are used to label voxels based on their texture features

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Gabor Filtering and Classification

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Gabor filtering and SVM Classification are performed on subsurfaces

I.e. Let us define our shape as a set of vertices $S = \{P_i, i = 1, ..., I\}.$

Let us note T a set of triangles where $T = \{Tr_i, i = 1, ..., I\}$ and $Tr_j = \{P_1^j, P_2^j, P_3^j\}$

Then the entire surface is decomposed into N subsurfaces $S_k = \{Tr_l^k, l = 1, ..., N_k\}$

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To save computation time, two gabor filter banks located at 2 orthogonal planes (axial and coronal) are used

$$g_{\gamma,\omega}(x,y) = a^{\gamma}g(a^{\gamma}(x\cos(\omega\psi) + y\sin(\omega\psi)),$$
$$a^{\gamma}(-x\sin(\omega\psi) + y\cos(\omega\psi))) \quad (1)$$

$$h_{\gamma,\omega}(y,z) = a^{\gamma} h(a^{\gamma}(y\cos(\omega\psi) + z\sin(\omega\psi)),$$
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$$(\gamma = 0, \dots, \Gamma - 1 \ \omega = 0, \dots, \Omega - 1)$$

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$$\left\{\hat{G}_{\gamma,\omega}^{real}(\vec{v})\right\}, \ \left\{\hat{G}_{\gamma,\omega}^{img}(\vec{v})\right\}, \left\{\hat{H}_{\gamma,\omega}^{real}(\vec{v})\right\}, \ \left\{\hat{H}_{\gamma,\omega}^{img}(\vec{v})\right\}$$

Gabor features are then compiled into a vector $T(\vec{v})$

This vector is then used to classify the voxels as organ and non organ using KSVM

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KSVM are first trained using the texture vectors coming from organ and non organ tissue

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The value returned by the KSVM is then mapped to the interval [0, 1] to denote the probability of voxel v to belong to the organ

$$L(\vec{v}) = s\left(f\left(\vec{T}(\vec{v})\right)\right) = s\left(\sum_{i=1}^{m} \alpha_i l_i K\left(\vec{T}_i, \vec{T}(\vec{v})\right) + b\right)$$

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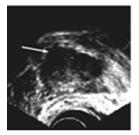
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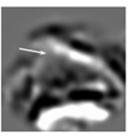
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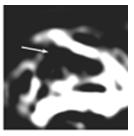
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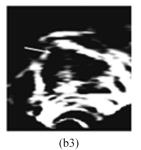
(a)

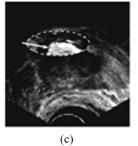


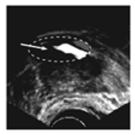
(b1)



(b2)







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Since texture varies greatly along prostate boundaries

Instead of using a single G-SVM, one G-SVM is associated to each subsurface S_k in the deformable model

Number of subsurfaces should be limited (essentially because of time) for use in clinical applications

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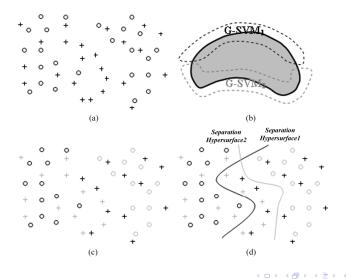
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Once results of the G-SVM have been computed for the whole surface, an external energy term is computed

$$E^{ext}(\vec{P_i}) = w_{Sum}E_{Sum}(\vec{P_i}) + w_{Dist}E_{Dist}(\vec{P_i})$$

$$\mathbf{E}_{Sum}(\vec{P}_i) = \left(\left(\frac{\sum_{\forall \vec{v} \in N(\vec{P}_i)} L(\vec{v};j))}{\sum_{\forall \vec{v} \in N(\vec{P}_i)} 1} \right) - 0.5 \right)^2$$

$$E_{Dist}(\vec{P}_i) = \frac{\left(d(\vec{C}_P, \vec{P}_i) - d(\vec{C}_{NP}, \vec{P}_i) \right)^2}{R^2}$$

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